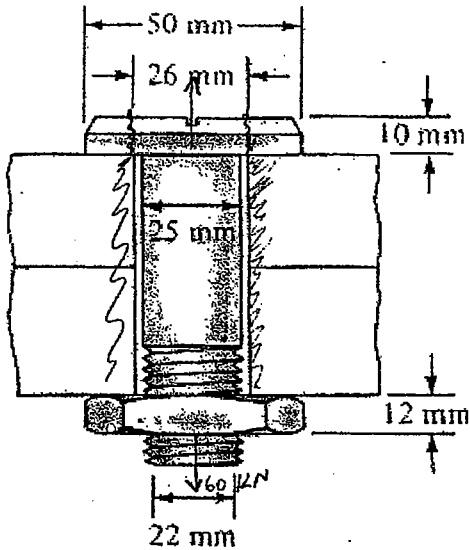


**PROB-1 (35)**



Two plates are fastened by a bolt as shown in the Figure. The nut is tightened to cause a tensile load in the shank (unthreaded part) of the bolt of 60 kN. Determine (a) the shearing stress in the threads; (b) the shearing stress in the head of the bolt; (c) the bearing stress between the head of the bolt and the plate; and (d) the normal stress in the bolt shank.

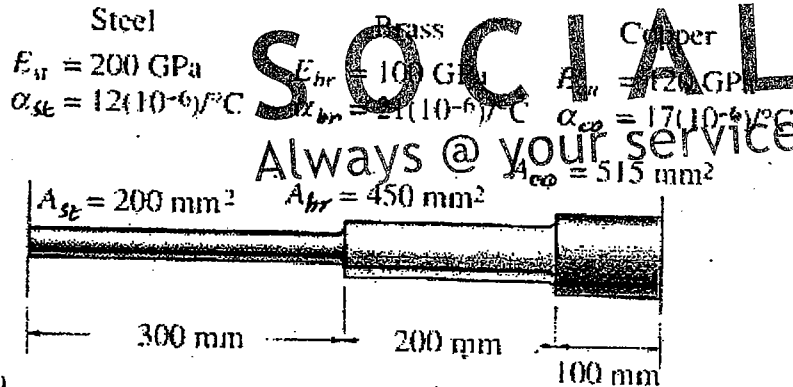
$$\tau = \frac{60 \times 10^3}{\pi (26)(10)} = 23.46 \text{ MPa}$$

$$\tau = \frac{60 \times 10^3}{\pi (25)(10)} = 76.39 \text{ MPa}$$

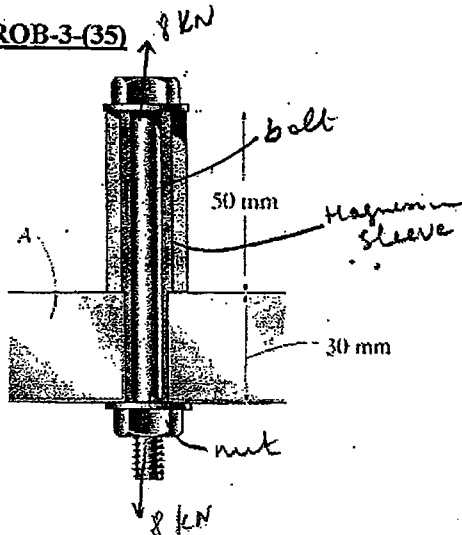
*(ultimate stress)*

**PROB-2-(30)**

Three bars each made of different materials are connected together and placed between two walls when the temperature is  $T_1 = 12^\circ\text{C}$ . Determine the force exerted on the (rigid) supports when the temperature becomes  $T_2 = 18^\circ\text{C}$ . The material properties and cross-sectional area of each bar are given in the Figure below.

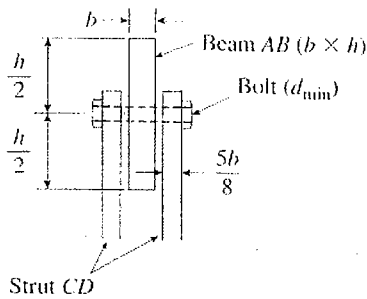
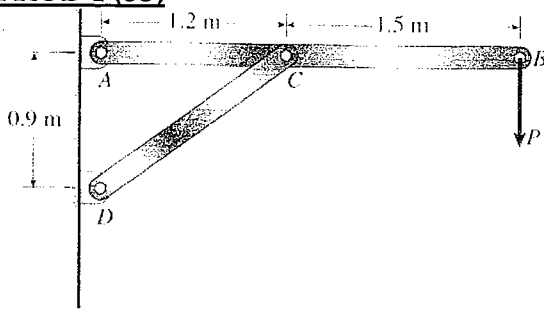


**PROB-3-(35)**



The 8-mm-diameter bolt is made of an aluminum alloy. It fits through a magnesium sleeve that has an inner diameter of 12 mm and an outer diameter of 20 mm. If the original lengths of the bolt and sleeve are 80 mm and 50 mm, respectively, determine the strains in the sleeve and the bolt if the nut on the bolt is tightened so that the tension in the bolt is 8 kN. Assume the material at A is rigid.  $E_{al} = 70 \text{ GPa}$ ,  $E_{mg} = 45 \text{ GPa}$ .

**PROB-1 (35)**



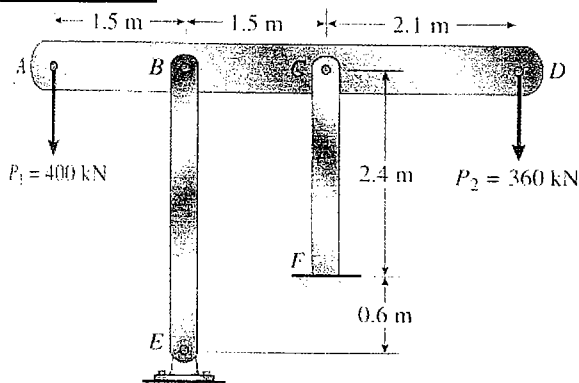
(b)

A horizontal beam  $AB$  with cross-sectional dimension ( $b = 19$  mm)  $\times$  ( $h = 200$  mm) is supported by an inclined strut  $CD$  and carries a load  $P = 12$  kN at joint  $B$  (see Figure). The strut, which consists of two bars each of thickness  $5b/8$ , is connected to the beam by a bolt passing through the three bars meeting at joint  $C$  [see figure part (b)].

(a) If the allowable shear stress in the bolt is 90 MPa, what is the minimum required diameter  $d_{min}$  of the bolt at  $C$ .

(b) If the allowable bearing stress in the bolt is 130 MPa, what is the minimum required diameter  $d_{min}$  of the bolt at  $C$ .

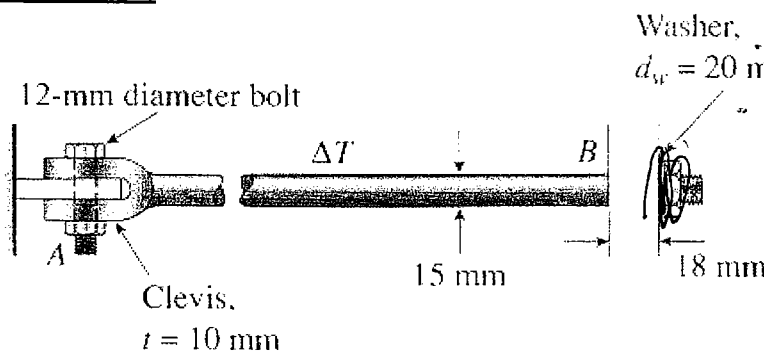
**PROB-2 (35)**



The horizontal rigid beam  $ABCD$  is supported by vertical bars  $BE$  and  $CF$  and is loaded by two vertical forces acting at points  $A$  and  $D$ , respectively (see figure). Bars  $BE$  and  $CF$  are made of steel ( $E = 200$  GPa) and have cross-sectional areas  $A_{BE} = 11,100$  mm<sup>2</sup> and  $A_{CF} = 9,280$  mm<sup>2</sup>. The distances between various points on the bars are shown in the figure.

Determine the vertical displacements of points  $A$  and  $D$ .

**PROB-3- (30)**



A steel rod of 15-mm diameter is held snugly (but without any initial stresses) between rigid walls by the arrangement shown in the figure. (For the steel rod, use  $\alpha = 12 \times 10^{-6}/^\circ\text{C}$  and  $E = 200$  GPa.)

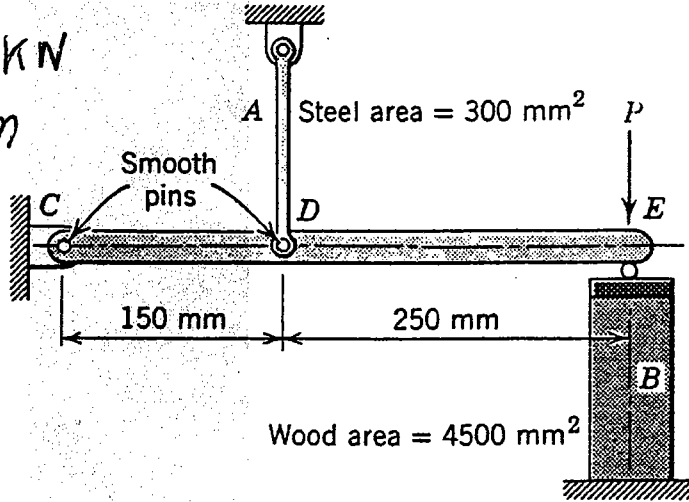
(a) Calculate the temperature drop  $\Delta T$  (degrees Celsius) at which the average shear stress in the 12-mm diameter bolt becomes 45 MPa.

(b) Determine the average bearing stresses in the bolt and clevis at  $A$  and the washer ( $d_w = 20$  mm) and wall ( $t = 18$  mm) at  $B$ .

**PROB-1-(35)**

The axial stresses are 12 MPa in the wood post B and 150 MPa in the steel bar A. Determine (a) The load P; (b) The minimum diameter for pin C if it is in single shear and the shearing stress is limited to 70 MPa; (c) The minimum diameter for pin D if it is in double shear and the shearing stress is limited to 50 MPa.

$P = 70.875 \text{ kN}$   
 $d_c = 22.62 \text{ mm}$   
 $d_D = 23.94 \text{ mm}$

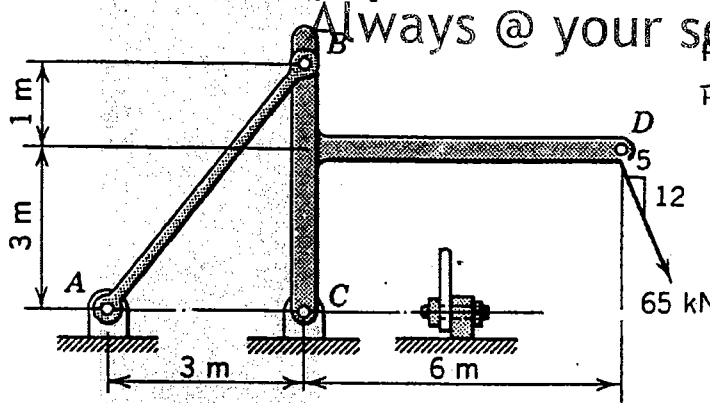


a)  $F_{AD} = 45 \text{ kN}$   
 $F_B = 54 \text{ kN}$   
 $\sum M_C = 0 \rightarrow P = 70.875$   
 b)  $C_y = 28.125 \downarrow$   
 $A_v = \frac{\pi}{4} D^2 \cdot \tau = 70$   
 $\Rightarrow D = 22.62$   
 c)  $\tau = \frac{F_{AD}}{2A_v}$   
 $A_v = \frac{\pi}{4} D^2$   
 $D = 23.93 \text{ mm}$

**PROB-2-(30)**

The tie rod AB has a cross-sectional area of 950 mm<sup>2</sup>. The cross-sectional area of pin C is 1850 mm<sup>2</sup>. Both the tie rod and the pin are made of steel for which the ultimate normal stress is 450 MPa and ultimate shearing stress is 270 MPa. Determine (a) The factor of safety in rod AB; (b) The factor of safety in pin C.

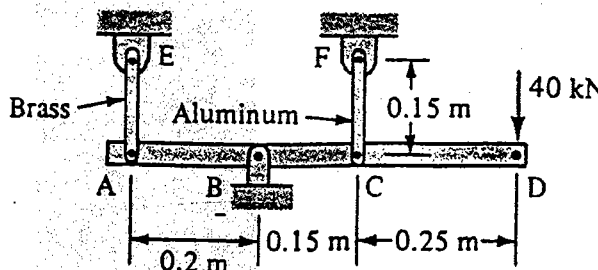
a)  $FS = 2.36$   
 b)  $FS = 2.26$



$F_{AB} = 181.25 \text{ kN}$   
 $F_C = 205 \text{ kN}$   
 $\sigma_{all} = 190.78$   
 $\Rightarrow F.S. = 2.36$   
 $\tau_{all} = 110.81$   
 $\Rightarrow F.S. = 2.4$

**PROB-3-(35)**

In the assembly shown below, brass rod AE ( $E_b = 105 \text{ GPa}$ ) and aluminum rod CF ( $E_a = 70 \text{ GPa}$ ) each have a cross-sectional area of 500 mm<sup>2</sup>. Determine the displacement of end D of the rigid member ABCD that would be caused by a 40 kN load.

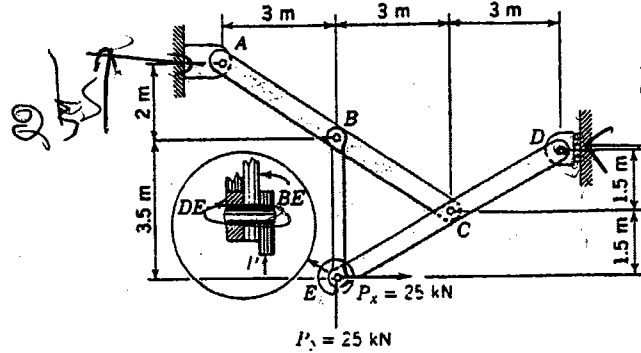


$\delta_D = 0.332 \text{ mm}$

$-0.2 F_E + 0.15 F_C = 16$

**PROB-1-(30)**

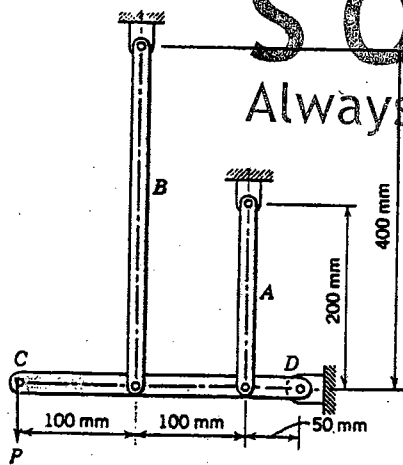
Member BE of the pin-connected structure shown below is a 25 X 8 mm rectangular bar. The load P is applied to the pin at E as shown below. The pin at E has a diameter of 30mm. Determine a) the axial stress in BE, and b) the shearing stress in the pin at E.



$\sigma = 150 \text{ MPa}$   
 $\tau_E = 21.22 \text{ MPa}$   
 $\tau_E = 50.02 \text{ MPa}$

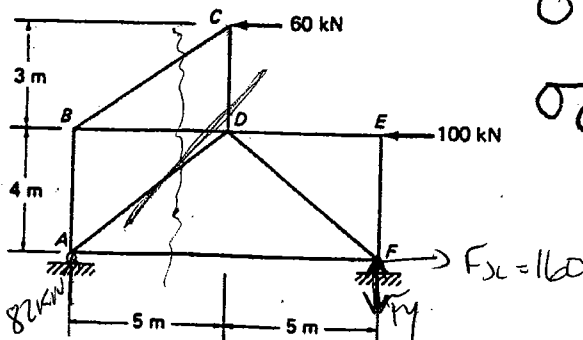
**PROB-2-(40)**

Bar CD of the pin-connected structure shown below is to be considered rigid. If temperature in bar A ( $E = 200 \text{ GPa}$ ,  $A = 150 \text{ mm}^2$ ,  $\alpha = 11.9 \times 10^{-6}/^\circ\text{C}$ ) increases by  $100^\circ\text{C}$  and the temperature in bar B ( $E = 100 \text{ GPa}$ ,  $A = 200 \text{ mm}^2$ ,  $\alpha = 17.6 \times 10^{-6}/^\circ\text{C}$ ) increases by  $50^\circ\text{C}$  after the 24 kN load P is applied. Determine the vertical displacement of point C.



**PROB-3-(30)**

For the truss shown below, determine the stresses in members AD and CD. Given  $A_{CD} = 200 \text{ mm}^2$  and  $A_{AD} = 150 \text{ mm}^2$ .

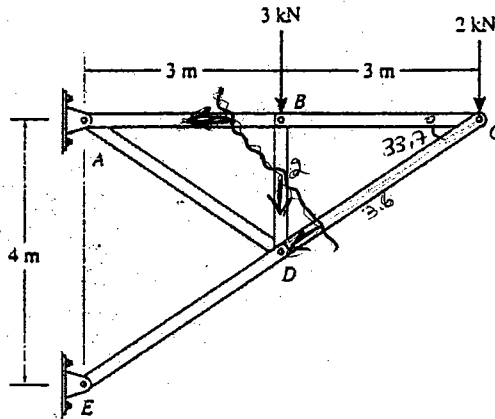


$\sigma_{AD} = -490.91 \text{ MPa}$   
 $\sigma_{CD} = 180 \text{ MPa}$

PROB-1-(25)

For the truss shown below, determine the stresses in members AB, BD, and CD. Given  $A_{AB} = 200 \text{ mm}^2$ ,  $A_{CD} = 150 \text{ mm}^2$ , and  $A_{BD} = 125 \text{ mm}^2$ .

$\sigma_{BD} = -24 \text{ MPa}$   
 $\sigma_{CD} = -24.04 \text{ MPa}$   
 $\sigma_{AB} = +15.0 \text{ MPa}$



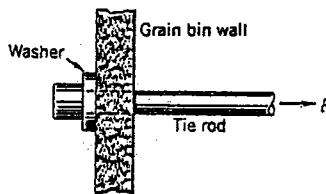
$F_{AB} = 3 \text{ kN}$   
 $F_{CD} = -3.605 \text{ kN}$   
 $F_{BD} = -3 \text{ kN}$

PROB-2-(40)

The tie rod shown below has a diameter of 40 mm and is used to resist the lateral pressure against the walls of a grain bin. If the tensile stress in the rod is 70 MPa, determine: a) The diameter of the washer that must be used if the bearing stress on the wall is not to exceed 3.0 MPa. b) The average shearing stress in the head of the rod if the head has a diameter of 80 mm and a thickness of 60 mm.

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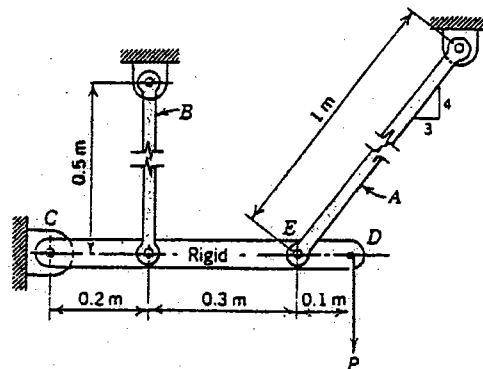
$P = (70) \left( \frac{\pi}{4} \right) (40)^2$   
 $= 87.96 \text{ kN}$



$D = 197.32 \text{ mm}$       $A_b = \frac{\pi D^2}{4}$   
 $\tau = 11.67 \text{ MPa}$       $A_v = \pi(R)(t)$

PROB-3-(35)

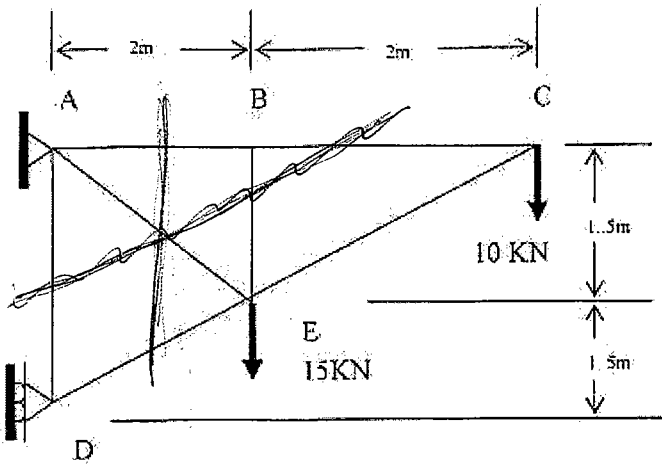
Bar A is made of aluminum with a modulus of elasticity of  $10.5 \times 10^3 \text{ ksi}$  and Bar B is made of steel with a modulus of elasticity of  $29 \times 10^3 \text{ ksi}$ . All bars have a rectangular cross section of 2.5 by 1.0 inches and are unstressed when P is zero. When load P is applied, the strain in A is found to be 0.0010. Determine the axial stresses and load P.



$\sigma_A = 10.5 \text{ ksi}$  ✓  
 $\sigma_B = 18.56 \text{ ksi}$   
 $P = 32.97 \text{ N}$

**PROB-1- (30)**

In the truss shown below, determine the stress in members AE, BE, and BC. Given that the members are 50 mm in diameter.



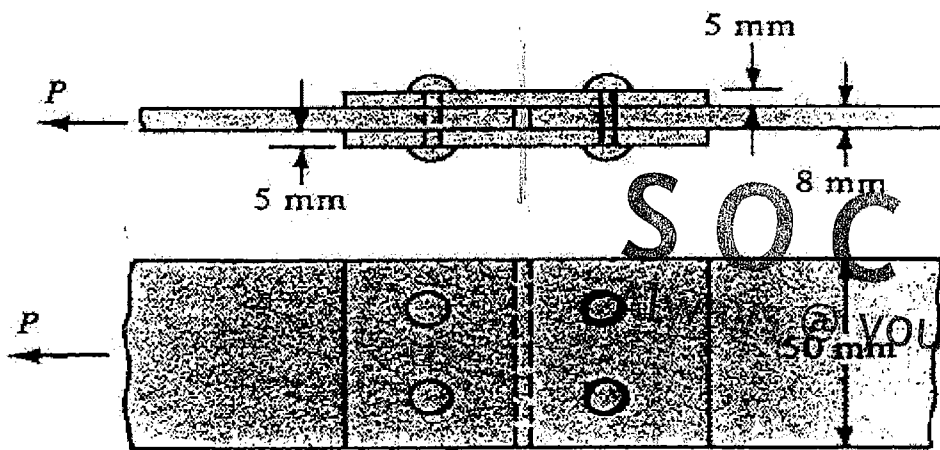
$$\sigma_{AE} = 6.37 \text{ MPa}$$

$$\sigma_{BE} = 0 \quad \checkmark$$

$$\sigma_{BC} = 6.79 \text{ MPa} \quad \checkmark$$

**PROB-2- (35)**

The butt joint shown below is fastened by four 15 mm diameter rivets. Determine the maximum load P if the maximum stresses are not to exceed 100 MPa in shear, 140 MPa in tension, and 210 MPa in bearing. Assume that the load is equally divided among the rivets.



$$P_{\sigma} = 22.4 \text{ kN}$$

$$P_{\tau} = 70.69 \text{ kN}$$

$$P_b = 113.4 \text{ kN}$$

$$USE P = 22.4 \text{ kN}$$

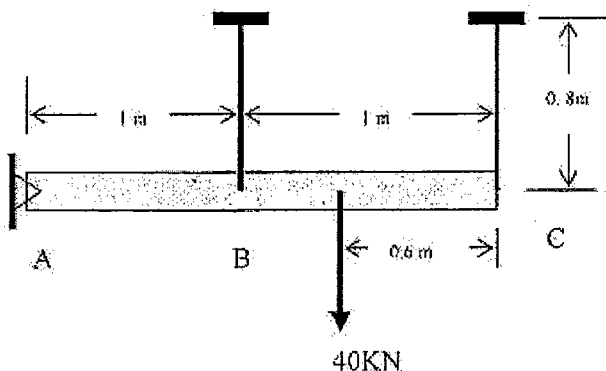
$$P_{SERVICE} = \frac{P}{4AV} \quad (AV = \frac{\pi}{4} 15^2)$$

$$A_L = (50 - 30)(8)$$

$$A_B = 2(5 + 8)(15)$$

**PROB-3- (35)**

A rigid horizontal bar ABC is supported by a hinge at A and by two steel cables at B and C, which are of equal length  $L = 0.8 \text{ m}$ , and area  $A = 140 \text{ mm}^2$ . Given  $E = 200 \text{ GPa}$  and a load of 40 kN is applied as shown. Determine the stress in each cable.



$$\sigma_B = 80 \text{ MPa} \quad \checkmark$$

$$\sigma_C = 160 \text{ MPa} \quad \checkmark$$

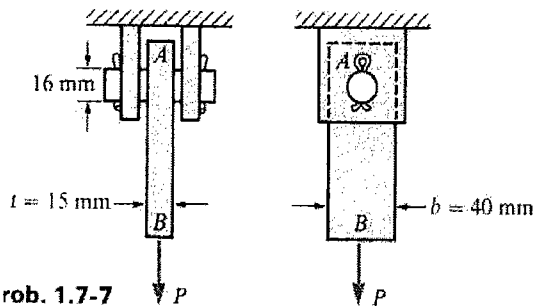
$$F_B + 2F_C = 56$$

$$\delta_C = 2\delta_B \Rightarrow F_C = 2F_B$$

$$F_B = 11.2 \text{ kN}$$

$$F_C = 22.4 \text{ kN}$$

**PROB-1 (35)**

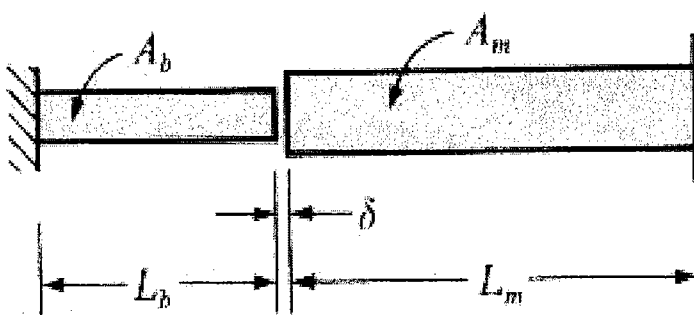


An aluminum bar  $AB$  is attached to its support by a 16 mm diameter pin at  $A$  (see figure). The thickness  $t$  of the bar is 15 mm, and its width  $b$  is 40 mm. If the allowable tensile stress in the bar is 150 MPa and the allowable shear stress in the pin is 85 MPa, find the allowable load  $P$ .

$P = 54 \text{ KN}$   
 $P = 34.18 \text{ KN}$

**PROB-2-(40)**

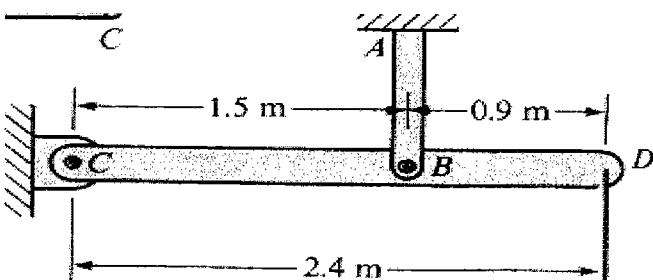
The bimetallic thermal control shown in the figure is made of a brass bar (length  $L_b = 0.75$  in. and cross-sectional area  $A_b = 0.10$  in.<sup>2</sup>) and a magnesium bar (length  $L_m = 1.30$  in. and cross-sectional area  $A_m = 0.20$  in.<sup>2</sup>). The two bars are arranged so that the gap between their free ends is  $\delta = 0.0040$  in. at room temperature. Calculate the following quantities: (a) the temperature increase  $\Delta T$  (above room temperature) at which the two bars come into contact, and (b) the stress  $\sigma$  in the magnesium bar when the temperature increase  $\Delta T$  is 300 °F. (Use the following material properties:  $\alpha_b = 10 \times 10^{-6} / ^\circ\text{F}$ ,  $\alpha_m = 14.5 \times 10^{-6} / ^\circ\text{F}$ ,  $E_b = 15 \times 10^6$  psi, and  $E_m = 6.5 \times 10^6$  psi.)



$0.004 = 10 \times 10^{-6} \Delta T \times 0.75 + 14.5 \times 10^{-6} \Delta T \times 1.30$   
 $0.004 = 7.64 \times 10^{-6} \Delta T$   
 $\Delta T = 523.57 \text{ } ^\circ\text{F}$   
 $0.004 = \alpha_b \Delta T L_b + \alpha_m \Delta T L_m$

**PROB-3-(25)**

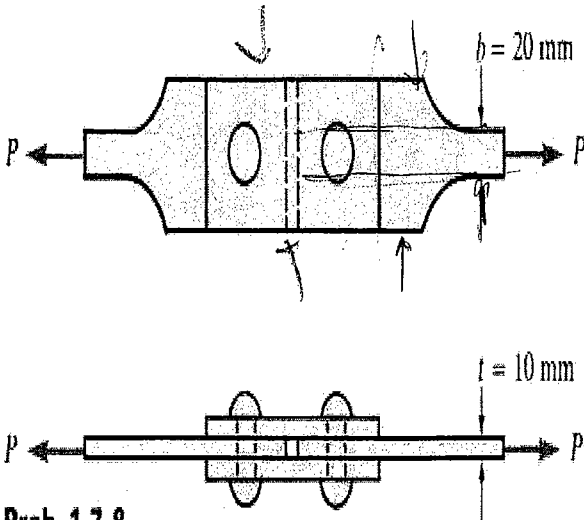
A horizontal bar  $CBD$  having a length of 2.4 m is supported and loaded as shown in the figure. The vertical member  $AB$  has a cross-sectional area of 550 mm<sup>2</sup>. Determine the magnitude of the load  $P$  so that it produces a normal stress equal to 40 MPa in member  $AB$ .



Prob. 1.2-2

$P = 13.75 \text{ KN}$

**PROB-1 (35)**



Two flat bars loaded by a tensile force  $P$  are spliced using two 15 mm diameter rivets (see figure). The bars have width  $b = 20$  mm and thickness  $t = 10$  mm. The bars are made of steel having an ultimate stress equal to 400 M Pa. The ultimate shear stress for the rivet steel is 180 M Pa. Determine the allowable load  $P$  if a safety factor of 3.0 is desired with respect to the ultimate load that the connection can carry. (Assume that the bars do not fail in tension at a cross section through a rivet, and disregard friction between the

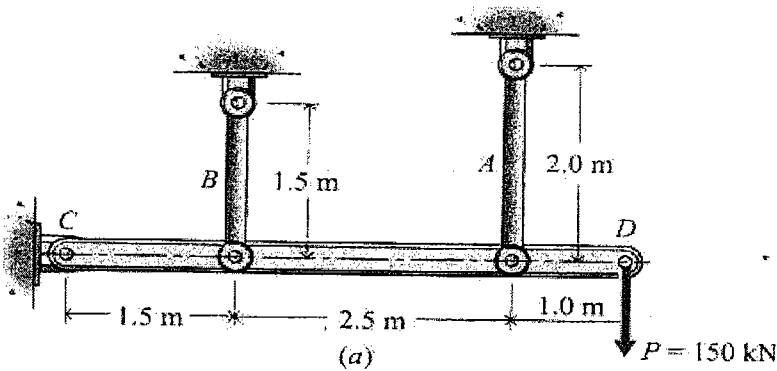
$P_0 = 6.66 \text{ kN}$   
 $P_G = 21.205 \text{ kN}$

Prob. 1.7-8

**PROB-2-(40)**

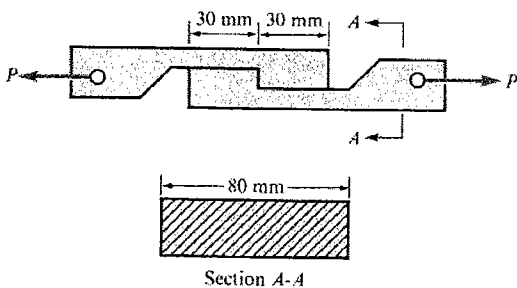
After a load  $P = 150$  kN is applied to the pin-connected structure shown in figure below, the temperature increases  $100$  °C. The thermal coefficients of expansion are  $22 \times 10^{-6}/\text{°C}$  for the aluminum alloy rod  $A$  and  $12 \times 10^{-6}/\text{°C}$  for the steel rod  $B$ . The moduli of elasticity of aluminum and steel are  $75$  G Pa and  $200$  G Pa, respectively. The cross-sectional area of members  $A$  and  $B$  are  $1000$  mm<sup>2</sup> and  $500$  mm<sup>2</sup>, respectively. If member  $CD$  is rigid, determine (a) The normal stresses in bars  $A$  and  $B$ . (b) The vertical component of the displacement of point  $D$ .

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a)  $\sigma_A = 210 \text{ MPa}$   
 $\sigma_B = 120 \text{ MPa}$   
 b)  $\delta_D = 15.15 \text{ mm}$

**PROB-3-(25)**

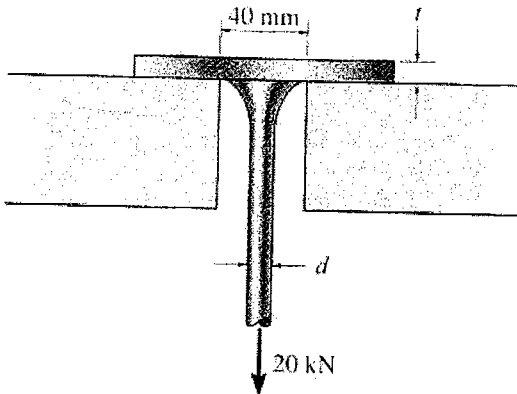


Two pieces of material are interlocked as shown in the figure and are pulled by forces  $P$ . If the ultimate stress in shear for the material is 38 M Pa, what force  $P$  is required to fracture the piece in shear.

$P = 182.4 \text{ kN}$



**PROB-1 (30)**

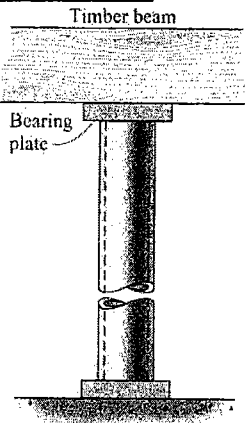


The suspended rod is supported at its end by a fixed-connected circular disk as shown in Figure. If the rod passes through a 40-mm-diameter hole, determine the minimum required diameter of the rod and the minimum thickness of the disk needed to support the 20-kN load. The allowable normal stress for the rod is  $\sigma_{allow} = 60$  MPa, and the allowable shear stress for the disk is  $\tau_{allow} = 35$  MPa.

$$\sigma = \frac{P}{A_c} \quad d = 20.60 \text{ mm} \quad t = 4.55 \text{ mm}$$

$$A_c = \pi R^2 \quad \text{or} \quad \frac{\pi D^2}{4} \quad \tau = \frac{P}{A_v} \quad A_v = (\pi)(R)(t)$$

**PROB-2 (40)**



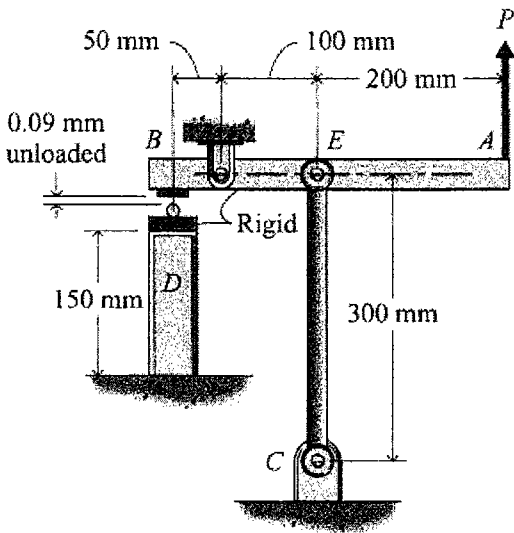
The steel ( $E_s = 200$  GPa) pipe column shown in Figure has an outside diameter of 150 mm and a wall thickness of 15 mm. The load imposed on the column by the timber beam is 150 kN. Determine

- (a) The average bearing stress at the surface between the column and the steel bearing plate.  $\sigma_b = 23.58$  MPa
- (b) The diameter of a circular bearing plate if the average bearing stress between the steel plate and the wood beam is not to exceed 3.25 MPa.

$$D = 242.41 \text{ mm} \quad A = \pi R^2$$

- (c) The change in the pipe thickness if  $\nu = 0.3, \delta t = 0.000531$  mm
- $$\gamma = -\frac{E_{LAT}}{E_{AX}} \quad \epsilon_{AX} = \frac{\delta D}{D} = \frac{P D}{D A E} = 0.000117$$
- $$\epsilon_{LAT} = 3.5 \times 10^{-5} = \frac{\delta t}{t} \Rightarrow \delta t = 0.000531$$
- where did the (-) go??*

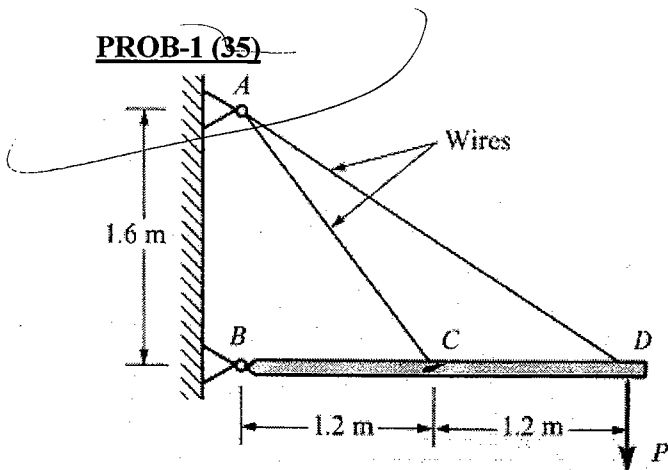
**PROB-3- (30)**



The load  $P$  produces an axial strain of 0.0075 m/m in the steel post  $D$  in the Figure; Determine the axial strain in the aluminum rod  $CE$  if there is a 0.09 mm clearance between  $B$  and  $D$  before the load  $P$  is applied.

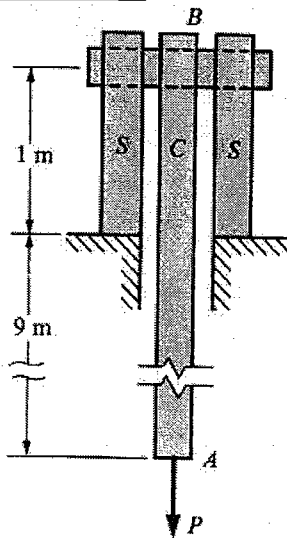
$$\epsilon_{CE} = 0.0081$$

**PROB-1 (35)**



A rigid bar  $BD$  is supported by a pin support at  $B$  and by two wires attached at  $C$  and  $D$  (see figure). The wires are identical except for length and are just taut (but free from stress) before the load  $P$  is applied. Find the tensile forces produced in the wires by a load  $P = 5000 \text{ N}$ .

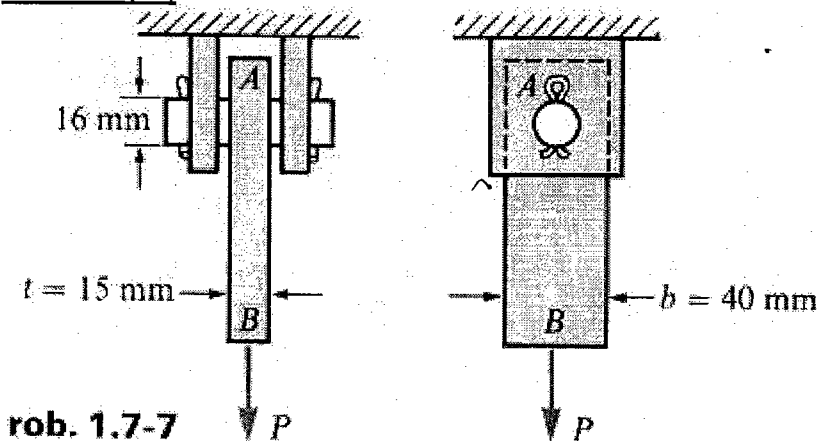
**PROB-2 (35)**



A copper bar  $AB$  under a tensile load  $P = 500 \text{ KN}$  hangs from a pin supported by two steel pillars (see figure). The copper bar has length  $10 \text{ m}$ , cross-sectional area  $8100 \text{ mm}^2$ , and modulus of elasticity  $E_c = 103 \text{ GPa}$ . Each steel pillar has height  $1 \text{ m}$ , cross-sectional area  $7500 \text{ mm}^2$ , and modulus of elasticity  $E_s = 200 \text{ GPa}$ . Determine the displacement of point  $A$ .

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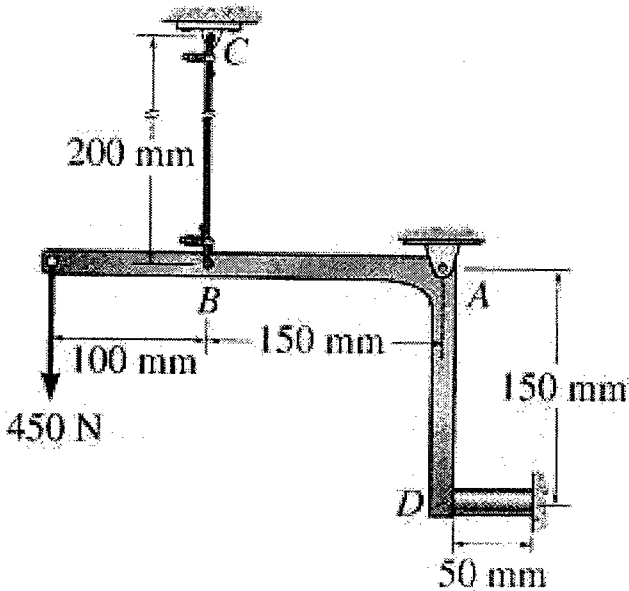
**PROB-3- (30)**



An aluminum bar  $AB$  is attached to its support by a  $16 \text{ mm}$  diameter pin at  $A$  (see figure). The thickness  $t$  of the bar is  $15 \text{ mm}$ , and its width  $b$  is  $40 \text{ mm}$ . If the allowable tensile stress in the bar is  $150 \text{ MPa}$  and the allowable shear stress in the pin is  $85 \text{ MPa}$ , and allowable bearing stress is  $75 \text{ MPa}$ , find the allowable load  $P$ .

rob. 1.7-7

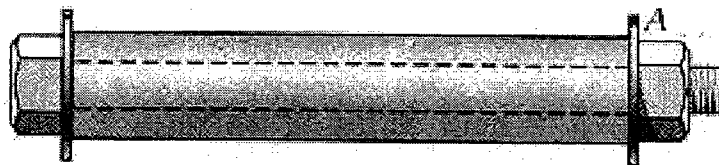
**PROB-1 (35)**



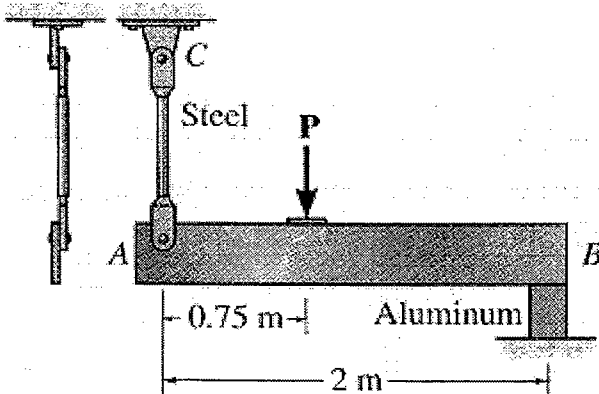
The rigid link is supported by a pin at *A*, a steel wire *BC* having an un-stretched length of 200 mm and cross-sectional area of 22.5 mm<sup>2</sup>, and a short aluminum block having an unloaded length of 50 mm and cross-sectional area of 40 mm<sup>2</sup>. If the link is subjected to the vertical load shown, determine the rotation of the link about the pin *A*. Report the answer in radians. Given that  $E_{st} = 200 \text{ GPa}$  and  $E_{al} = 70 \text{ GPa}$ .

**PROB-2-(30)**

The steel bolt has a diameter of 7 mm and fits through an aluminum sleeve as shown. The sleeve has an inner diameter of 8 mm and an outer diameter of 10 mm. The nut at *A* is adjusted so that it just presses up against the sleeve. If the assembly is originally at a temperature of  $T_1 = 20^\circ\text{C}$  and then is heated to a temperature of  $T_2 = 100^\circ\text{C}$ , determine the average normal stress in the bolt and the sleeve.  $E_{st} = 200 \text{ GPa}$ ,  $E_{al} = 70 \text{ GPa}$ ,  $\alpha_{st} = 14 \times 10^{-6}/^\circ\text{C}$ ,  $\alpha_{al} = 23 \times 10^{-6}/^\circ\text{C}$



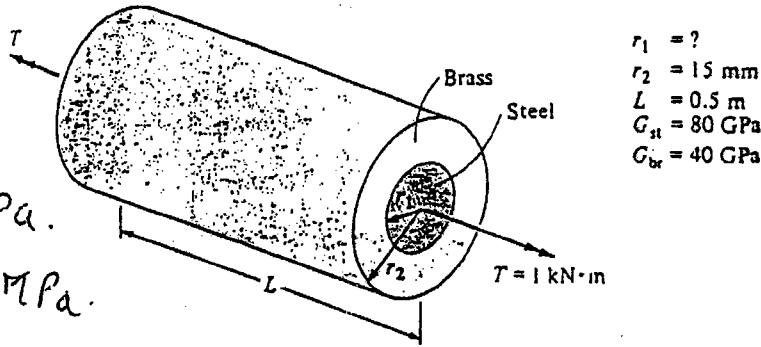
**PROB-3-(35)**



The rigid bar *AB* shown is supported by a steel rod *AC* having a diameter of 20 mm and an aluminum block having a cross-sectional area of 1800 mm<sup>2</sup>. Pins at *A* and *C* are 18-mm diameter pins. If the failure stress for the steel and aluminum is  $\sigma_{st(fail)} = 680 \text{ MPa}$  and  $\sigma_{AL(fail)} = 70 \text{ MPa}$ , respectively, and the failure shear stress for each pin is  $\tau_{fail} = 900 \text{ MPa}$ , determine the largest load *P* that can be applied to the bar. Apply a factor of safety of  $F.S. = 2$ .

PROB-1-(30)

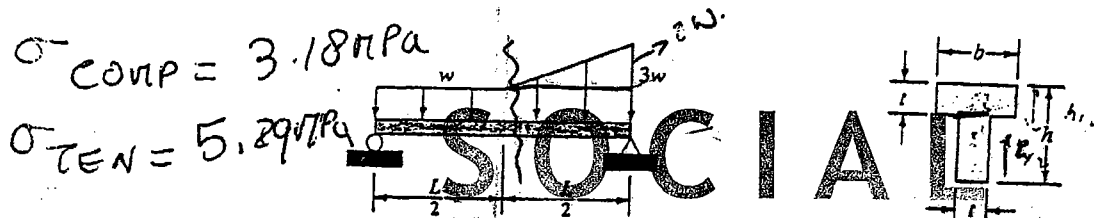
A composite bar consists of a steel core and a brass shell as indicated in the figure. Determine: a) The radius of the interface in order that each component carry half the torque. b) The maximum shear stresses in the steel and brass portions.



$r_1 = 11.40 \text{ mm}$   
 $\tau_1 = 214.85 \text{ MPa}$   
 $\tau_2 = 141.53 \text{ MPa}$

PROB-2-(35)

The T-beam section is subjected to the loading as shown below. Determine at midspan: a) The maximum compressive stress. b) The maximum tensile stress. Take  $L = 3 \text{ m}$ ,  $b = 0.15 \text{ m}$ ,  $h = 0.2 \text{ m}$ ,  $t = 0.05 \text{ m}$ , and  $W = 1.5 \text{ kN/m}$ .



$\sigma_{\text{COMP}} = 3.18 \text{ MPa}$   
 $\sigma_{\text{TEN}} = 5.29 \text{ MPa}$

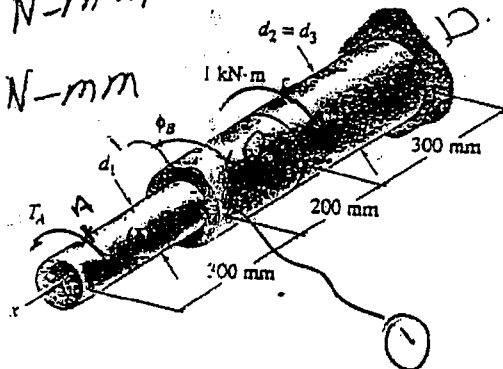
Tom Not  
 Suez  
 $M = 5.625 \text{ kNm}$   
 $\bar{y} = 0.15 \text{ m}$   
 $I = 6.65 \times 10^{-5} \text{ m}^4$

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PROB-3-(35)

The solid steel shaft AD shown below is subjected to applied torques at sections A and C. The shear modulus of elasticity  $G = 80 \text{ GPa}$  and the diameters of the shaft  $d_1 = 25 \text{ mm}$  and  $d_2 = d_3 = 40 \text{ mm}$ . If the angle of rotation at A is not to exceed  $|\phi_A|_{\text{allow}} = 0.0125$  radians in either direction, and the magnitude of the shear stress is not to exceed  $\tau_{\text{allow}} = 70 \text{ MPa}$  anywhere in the shaft. Determine: a) The minimum torque  $T_A$  that must be applied at end A. b) The maximum torque  $T_A$  that may be applied at end A.

MAX  $T_A = 2.24 \times 10^5 \text{ N-mm}$   
 MIN  $T_A = 1.20 \times 10^5 \text{ N-mm}$

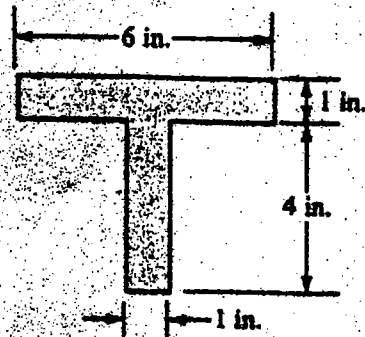
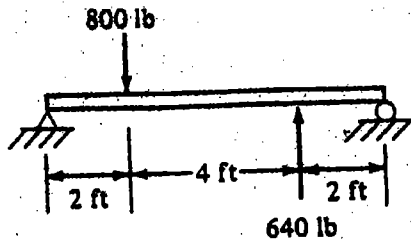


**PROB-1-(40)**

For the beam and loading shown below, calculate at midspan: i) The maximum compressive stress; and ii) The maximum tensile stress.

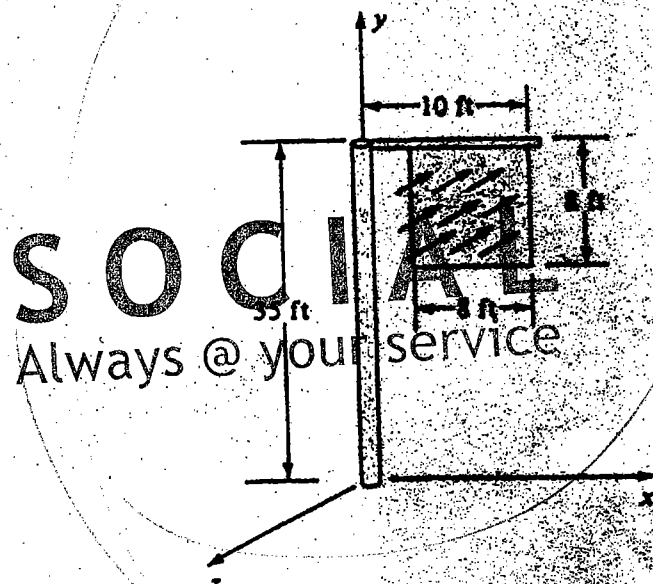
$\sigma_{TOP} = -138.24 \text{ PSI} ; \sigma_{BOT} = 32265 \text{ PSI}$

*Handwritten mark*



**PROB-2-(35)**

The circular steel column shown below supports a sign board 8 ft by 8 ft that is subjected to a uniform loading of 30 lb/ft<sup>2</sup>. Determine the required diameter of the column if the allowable shear stress due to torsional loading is limited to 10 ksi.



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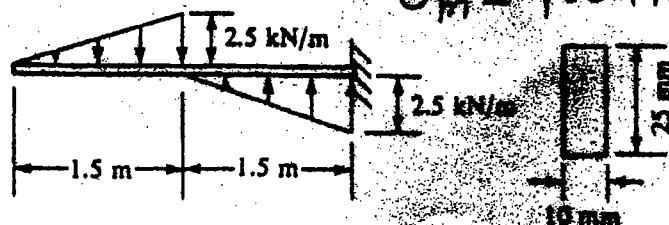
$d = 4.13''$

**PROB-3-(25)**

For the beam shown below, compute at midspan, the maximum bending stress.

$\sigma_m = 900 \text{ MPa}$

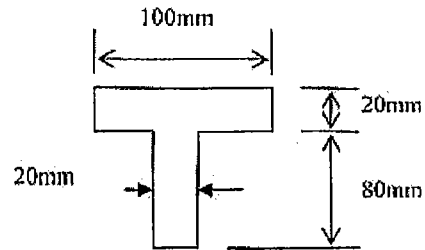
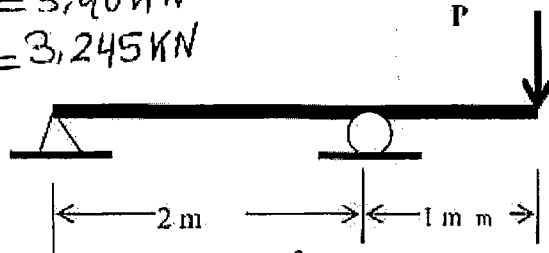
*Handwritten mark*



**PROB-1-(35)**

For the beam and cross-section shown below, calculate the load P based on an allowable stress of 40 MPa in tension and 70 MPa in compression.

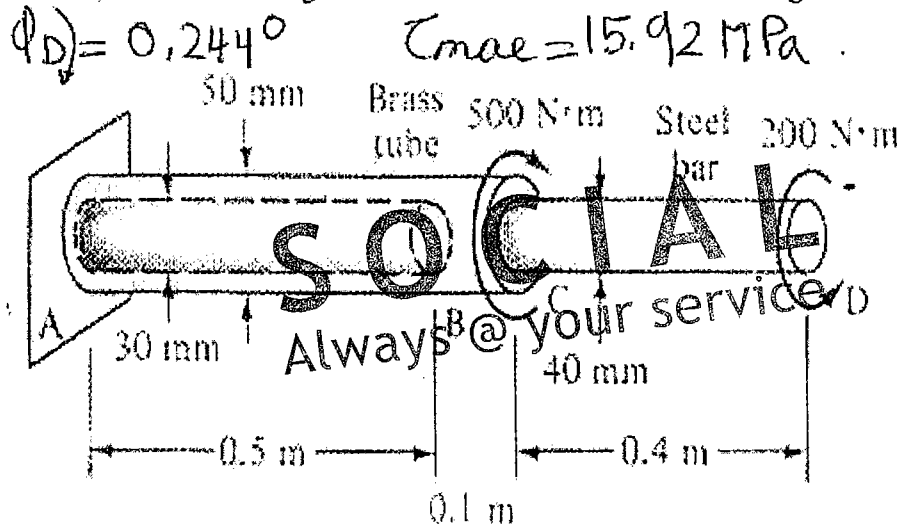
$P_T = 3,90 \text{ kN}$   
 $P_C = 3,245 \text{ kN}$



USE  $P = 3,245 \text{ kN}$

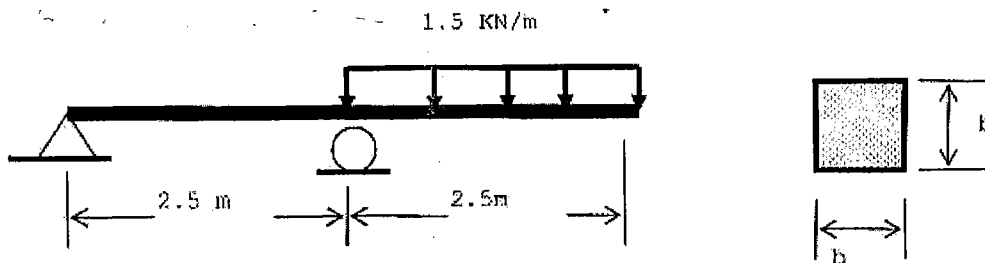
**PROB-2-(30)**

The circular shaft shown below is subjected to torques at C and D. Given that  $G_{\text{brass}} = 40 \text{ GPa}$  and  $G_{\text{steel}} = 80 \text{ GPa}$ , determine the angle of twist at D and the maximum shearing stress in the shaft.



**PROB-3-(35)**

The beam shown below has a square cross-section and carries the loading as shown. Calculate the required side dimension b of the square cross-section if the allowable bending stress is 12 MPa.

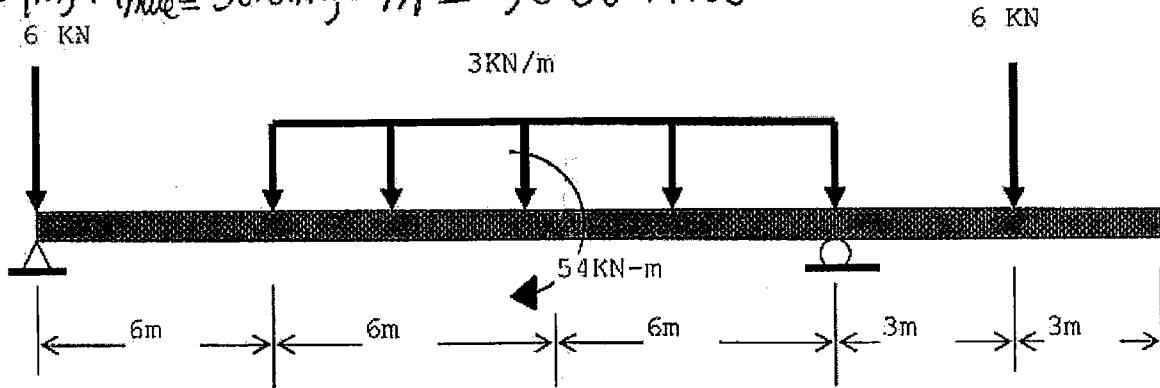


$b = 132,83 \text{ mm}$

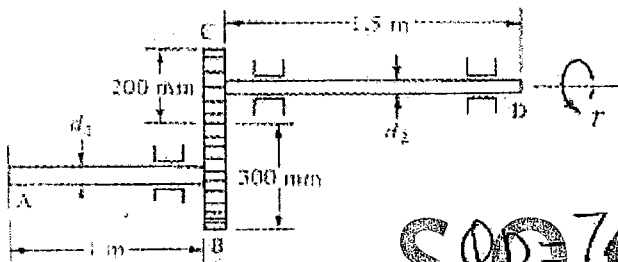
**PROB-1-(30)**

The cross section of the beam below is square of dimension 50x 50 mm. Determine the maximum stress at 9 m from the left hand pin support.

$X = 9m, M_{max} = 58,5 \text{ kN}\cdot\text{m}, \sigma_m = 2,808 \text{ MPa}$



**PROB-2(30)**

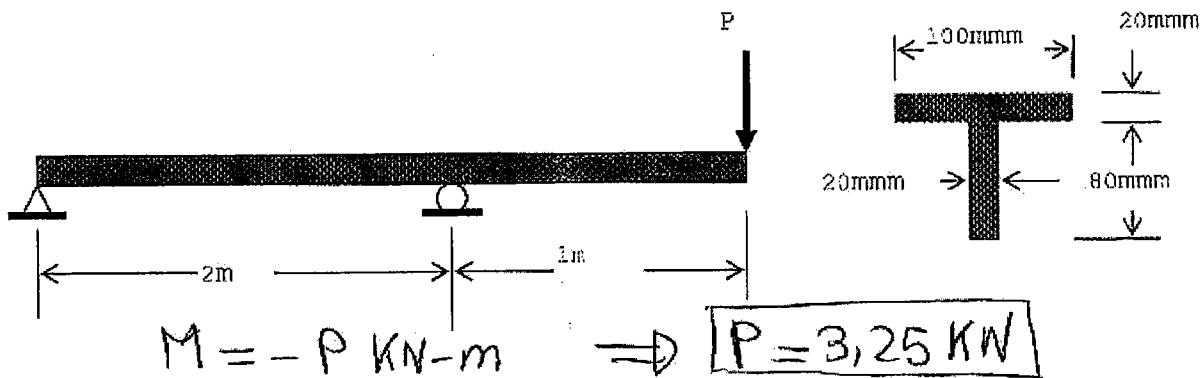


The two steel shafts ( $G = 80 \text{ GPa}$ ) are connected by gears and subjected to a torque of 400 N-m. Given that  $d_1 = 40 \text{ mm}$  and  $d_2 = 30 \text{ mm}$ , determine (a) the angle of rotation in degrees at D and (b) the maximum shearing stress in each shaft.

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 $\tau_{ABmax} = 47,75 \text{ MPa}$   
 $\tau_{CDmax} = 75,45 \text{ MPa}$

**PROB-3(40)**

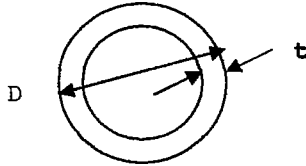
Determine the value of load P so that the maximum allowable stresses at the roller support does not exceed 40 MPa in tension and 70 MPa in compression.



**PROB-1-(30)**

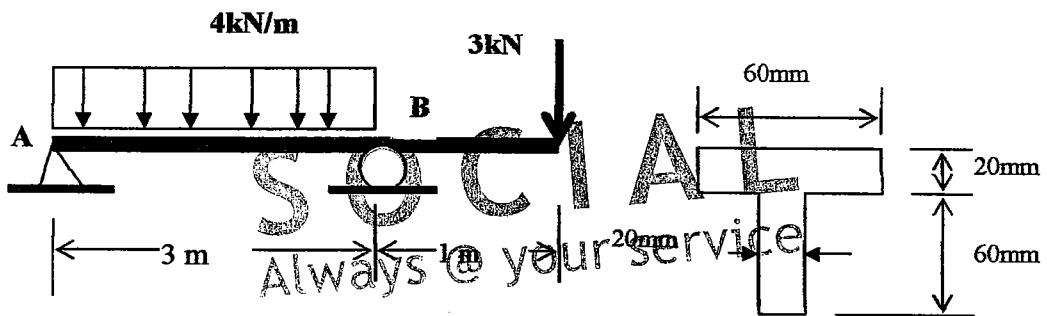
A 2 m long circular steel shaft must transmit a torque of 800 N-m. If the shaft is to be lightweight, it must be hollow. Assume the wall thickness is 0.1 times the diameter (see figure). If the maximum allowable shear stress in the shaft is 150 MPa; Determine:

- a) The required diameter in mm. b) The total angle of twist of one end of the shaft relative to the other.



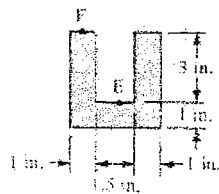
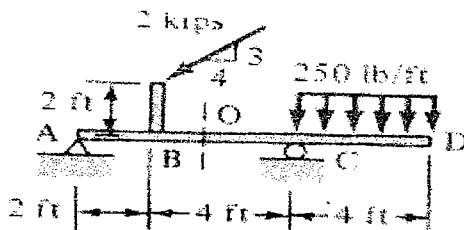
**PROB-2-(35)**

For the beam and cross-section shown below, calculate the maximum compressive and tensile stress at the midpoint between A and B.



**PROB-3-(35)**

For the beam and cross-section shown below, calculate the stress at point E and F of the cross section based on the moment value at the midpoint between B and C of the beam.

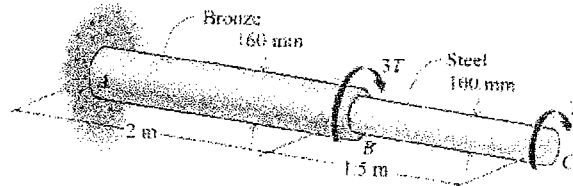




**PROB-1-(30)**

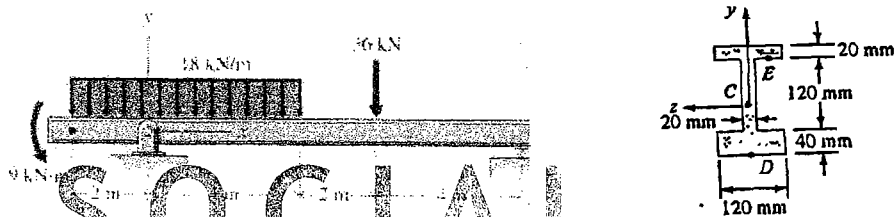
Q

A solid circular structural steel ( $G = 77 \text{ G Pa}$ ) shaft is securely fastened to a solid cold-rolled bronze shaft ( $G = 39 \text{ G Pa}$ ). For the steel, the allowable shearing stress is  $75 \text{ M Pa}$ ; for the bronze, the allowable shearing stress is  $150 \text{ M Pa}$ . The allowable angle of twist in the  $3.5\text{-m}$  length is  $2.5^\circ$ . Determine the maximum permissible value of the torque  $T$ .



**PROB-2-(40)**

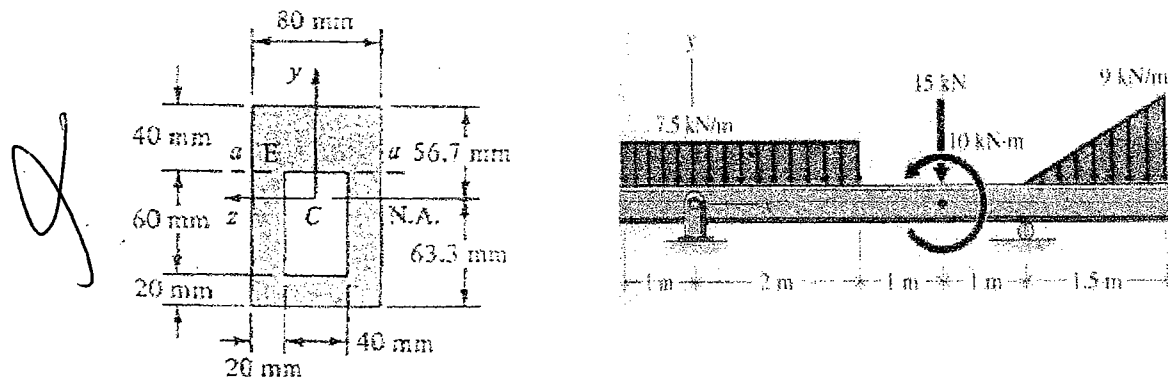
For the beam and cross-section shown below, for the moment value at midpoint between the supports, calculate the stresses at points D and E of the cross section.



**PROB-3-(30)**

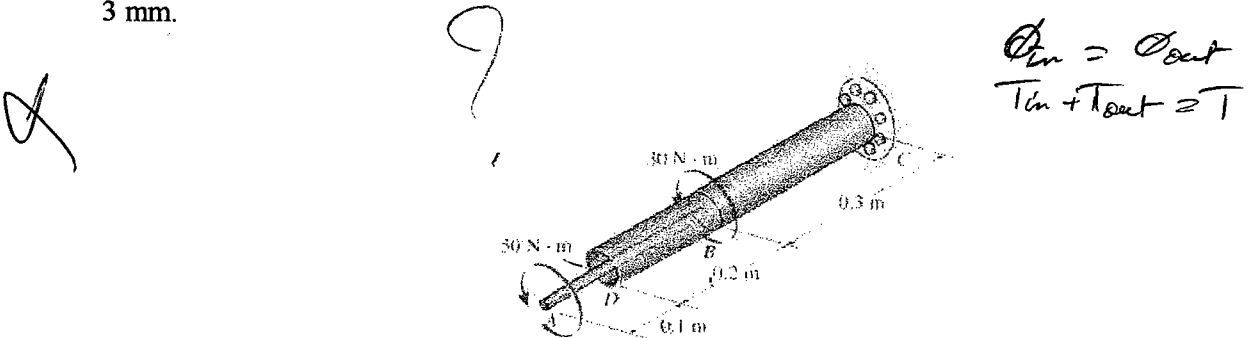
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For the beam and cross-section shown below, calculate the maximum compressive and tensile stress on the cross section based on the moment value at the midpoint between the two supports. Given  $I = 10.5 \times 10^6 \text{ mm}^4$ .



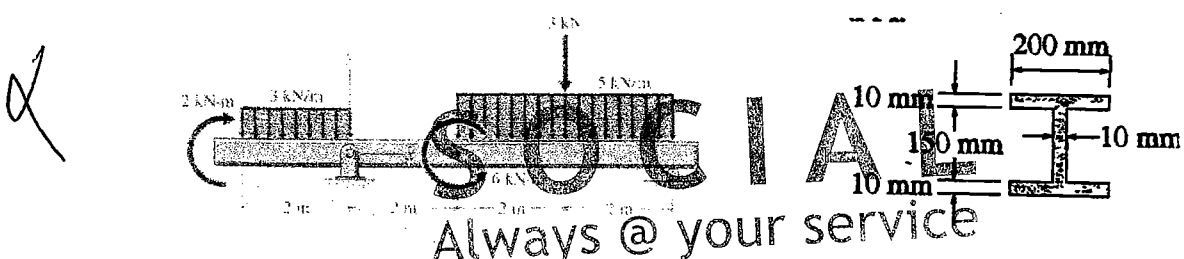
**PROB-1-(30)**

The shaft assembly shown below is made of A-36 steel ( $G = 77 \text{ GPa}$ ) and consists of a solid rod AB of 15 mm in diameter connected to the inside of a tube DBC using a rigid disk at B. Determine the angle of twist at A. The tube has an outer diameter of 30 mm and wall thickness of 3 mm.



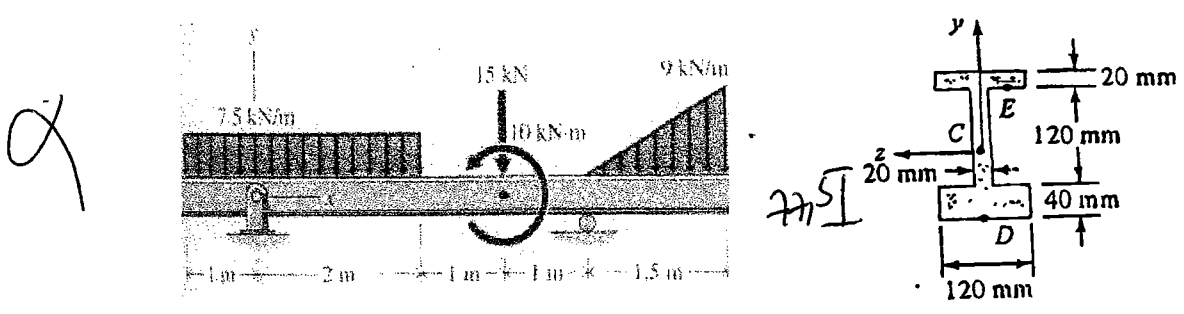
**PROB-2-(30)**

For the beam and cross-section shown below, for the moment value at midpoint between the supports, calculate the maximum compressive and tensile stresses.



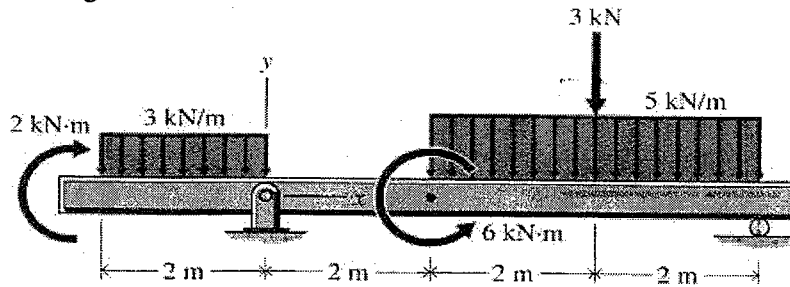
**PROB-3-(40)**

For the beam and cross-section shown below, for the moment value at midpoint between the supports, calculate the stresses at points D and E of the cross section.

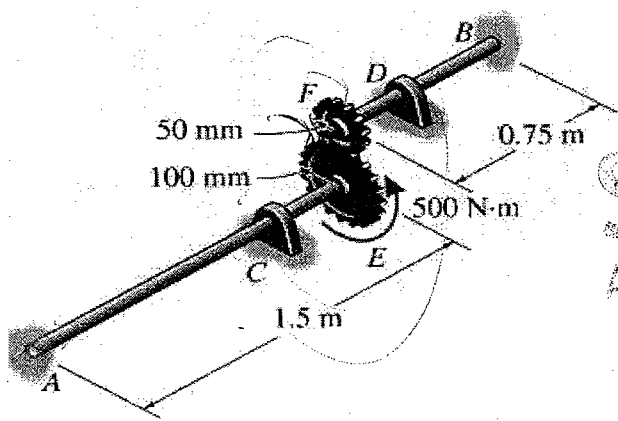


**PROB-1-(30)**

Draw the moment and shear diagrams for the beam shown below.



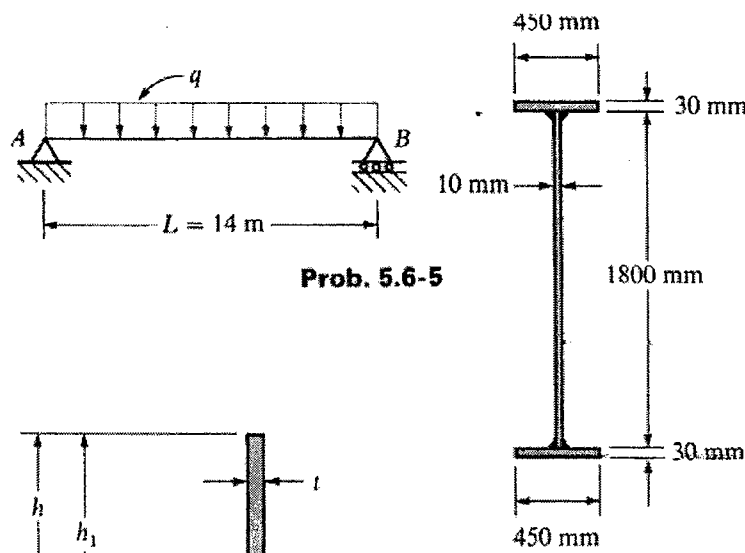
● **PROB-2(30)**



The two shafts are made of steel ( $G = 80 \text{ G Pa}$ ). Each has a diameter of 25 mm and they are connected using the gears fixed to their ends. Their other ends are attached to fixed supports at  $A$  and  $B$ . They are also supported by journal bearings at  $C$  and  $D$ , which allow free rotation of the shafts along their axes. If a torque of 500 N-m is applied to the gear at  $E$  as shown, determine the reactions at  $A$  and  $B$ .

● **PROB-3-(40)**

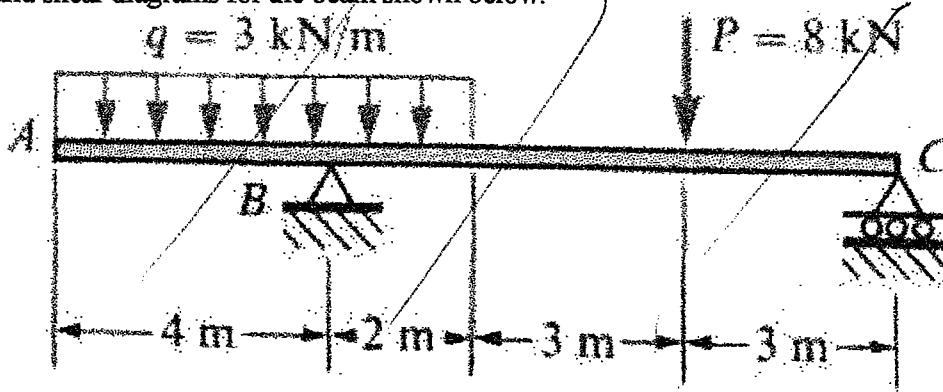
A simple beam  $AB$  with span length  $L = 14 \text{ m}$  supports a uniform load  $q$  that includes the weight of the beam. The beam is constructed of three plates welded together to form the cross section shown. Determine the maximum permissible load  $q$  based upon bending and shear if the allowable stresses are  $\sigma_{all} = 110 \text{ MPa}$  and  $\tau_{all} = 70 \text{ MPa}$ .



Prob. 5.6-5

**PROB-1-(30)**

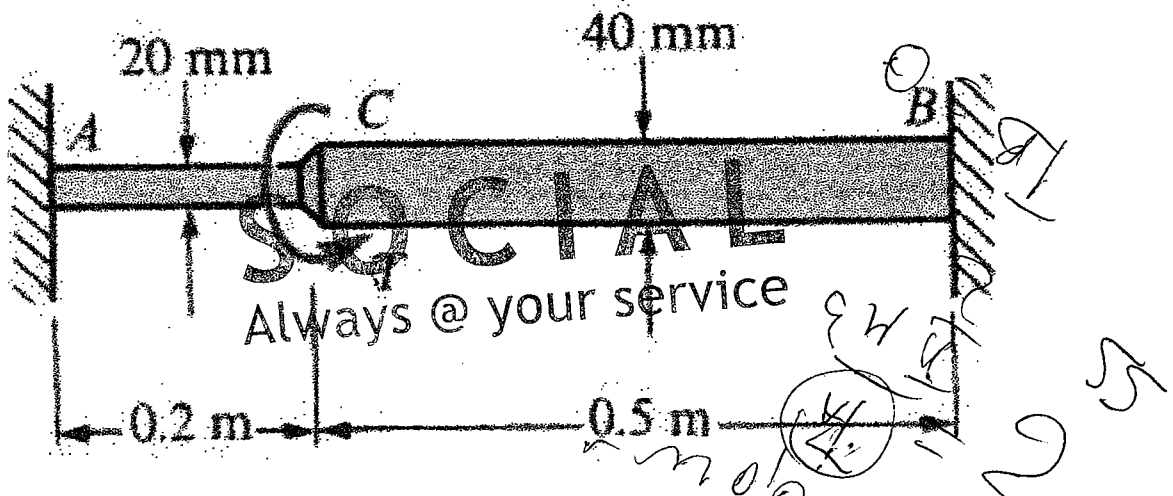
Draw the moment and shear diagrams for the beam shown below.



**PROB-2(35)**

The stepped shaft shown is made of solid circular cross section (see figure) and is held against rotation at the ends.

If the allowable stress in shear is 55 MPa, what is the allowable torque  $T$  that may be applied to the shaft at C?

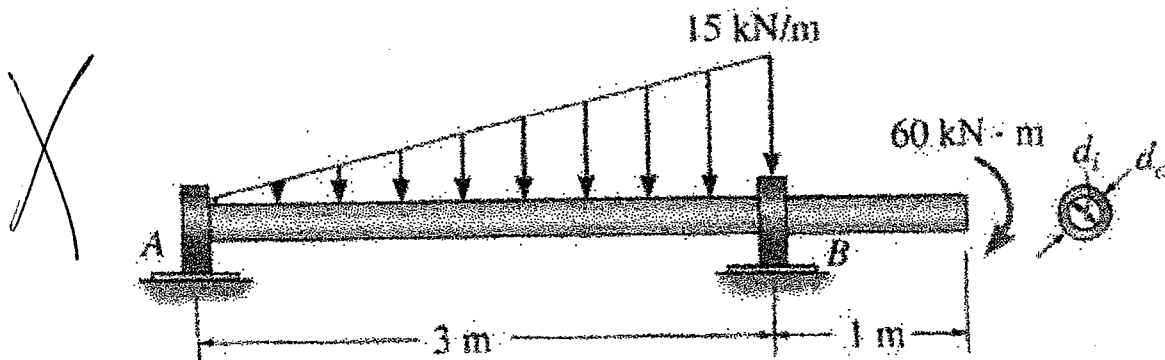


**PROB-3-(35)**

The tubular shaft is to have a cross section such that its inner diameter and outer diameter are related by

$d_i = 0.8 d_o$ . Support at A is considered as a pin and at B as a roller. Determine these required dimensions if the

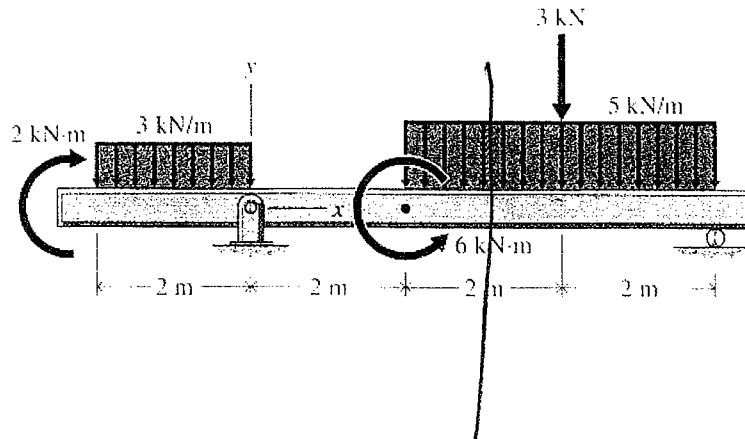
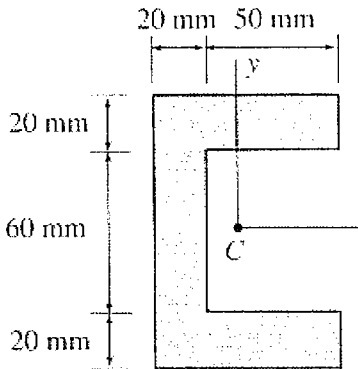
allowable bending stress is  $\sigma_{all} = 155 \text{ MPa}$ .





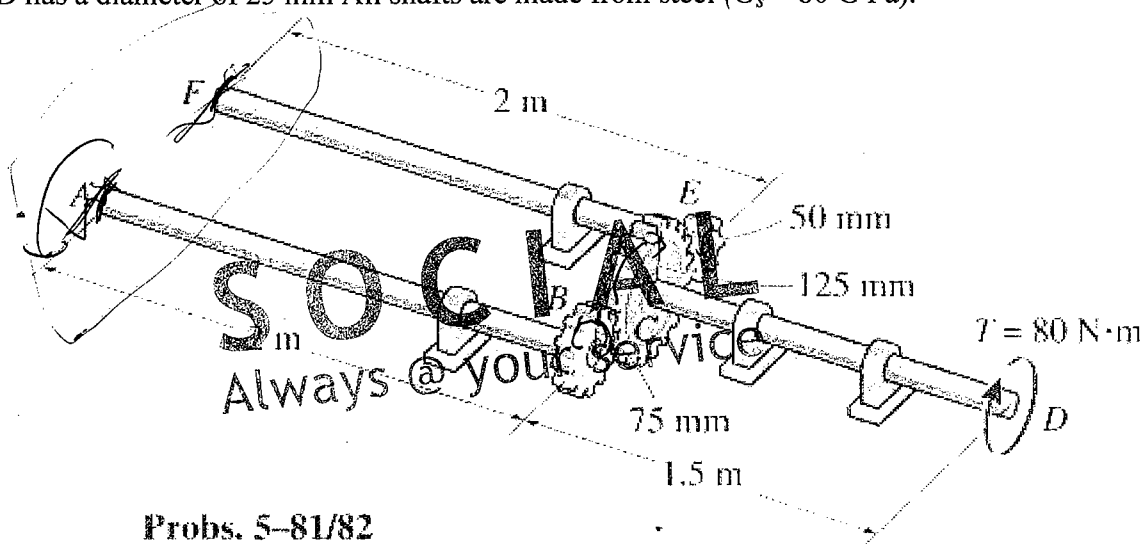
**PROB-1-(40)**

For the beam shown below determine the force acting on the top flange (70x20 mm) based on the value of the bending moment at mid span between the supports, The cross-section of the beam is shown to the right.



**PROB-2(35)**

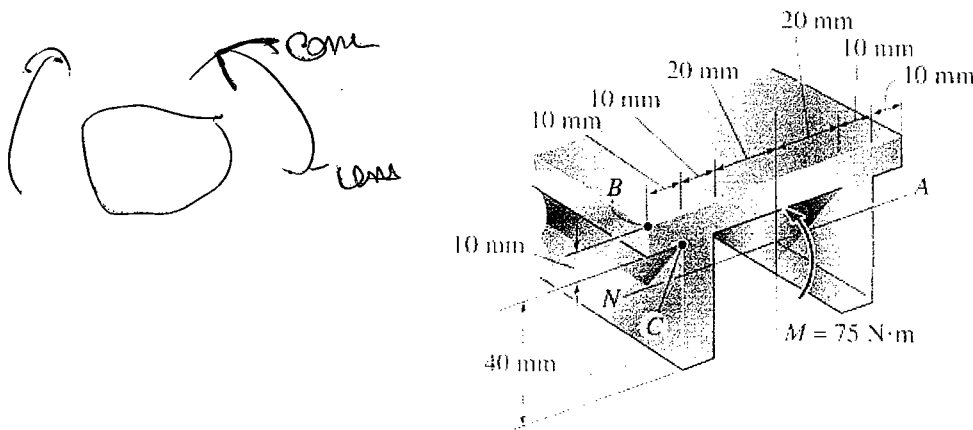
The two shafts *AB* and *EF* are fixed at their ends and fixed connected to gears that are in mesh with a common gear at *C*, which is fixed connected to shaft *CD*. If a torque of  $T = 80 \text{ N}\cdot\text{m}$  is applied to end *D*, determine a) the torque at *A* and *F* and b) the angle of twist of end *D*. Shaft *AB* has a diameter of 20 mm. Shaft *FE* has a diameter of 30 mm. Shaft *CD* has a diameter of 25 mm All shafts are made from steel ( $G_s = 80 \text{ GPa}$ ).



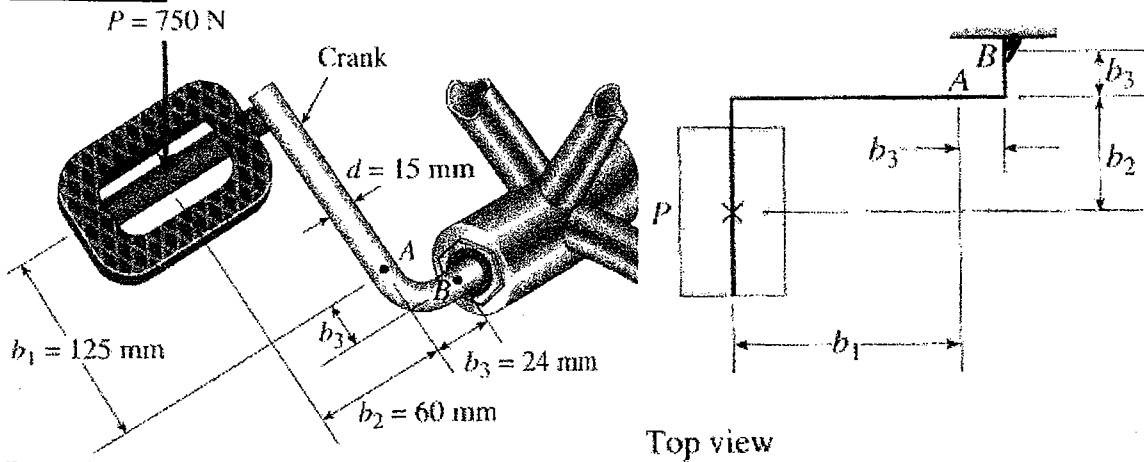
Probs. 5-81/82

**PROB-3-(25)**

The aluminum machine part is subjected to a moment of  $M = 75 \text{ N}\cdot\text{m}$ . Determine : a) the maximum tensile, b) the maximum compressive stress, and c) the stress at point *C* of the part.

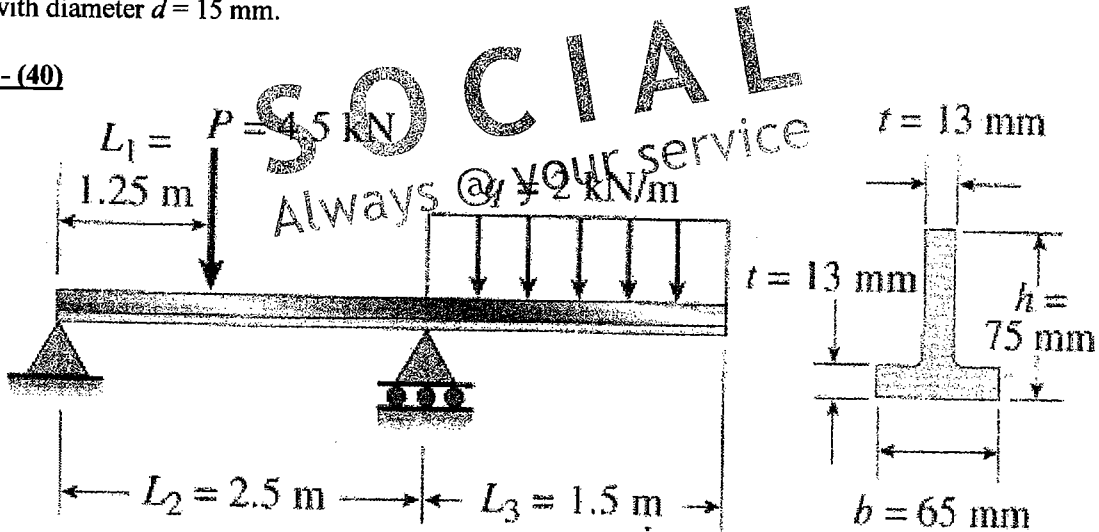


**PROB-1-(35)**



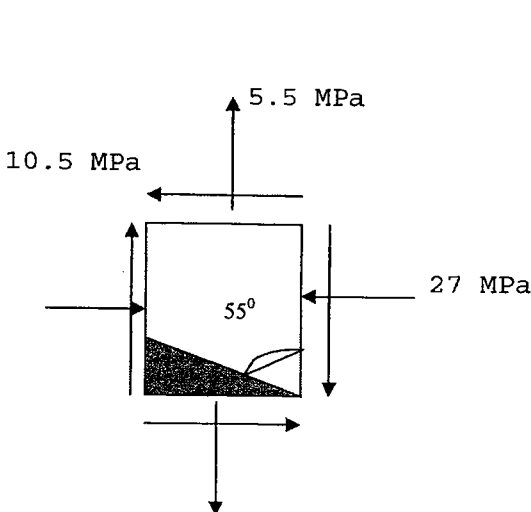
Draw the stress elements showing stresses at points *A* and *B* on the bicycle pedal crank shown in the figure. The pedal and crank are in a horizontal plane and points *A* and *B* are located on the top of the crank. The load  $P = 750$  N acts in the vertical direction and the distances (in the horizontal plane) between the line of action of the load and points *A* and *B* are  $b_1 = 125$  mm,  $b_2 = 60$  mm and  $b_3 = 24$  mm. Assume that the crank has a solid circular cross section with diameter  $d = 15$  mm.

**PROB-2-(40)**



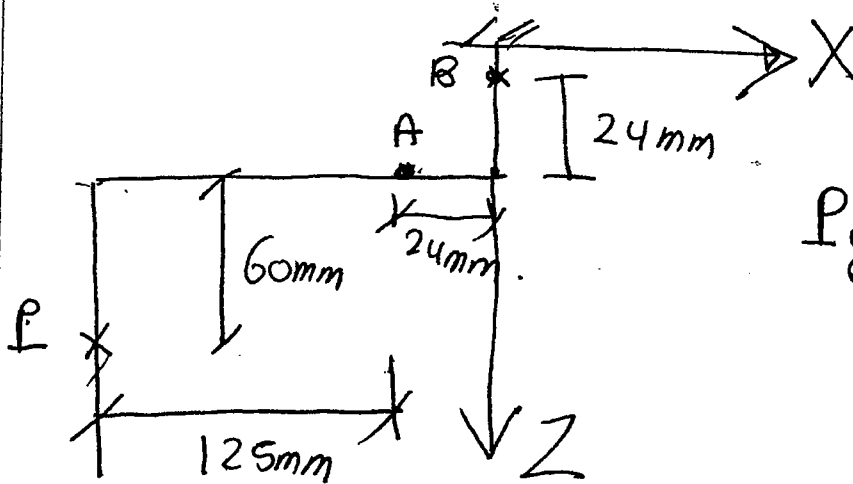
For the beam and cross section shown, determine the maximum tensile, compressive, and shearing stresses.

**PROB-3-(25)**



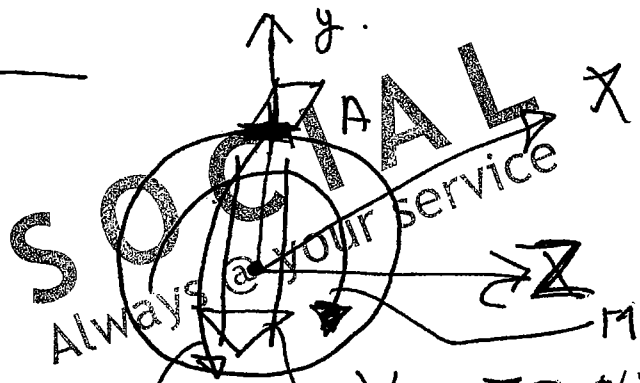
For the stress state shown to the left, determine: a) the normal and shearing stresses for the shaded area using the method of equilibrium; b) Draw the stress elements showing the principal stresses and maximum shearing stress.

$\Downarrow D = 15\text{mm} \Rightarrow R = 7.5\text{mm}$



$P_y = (-750\vec{j})\text{N}$

POINT A



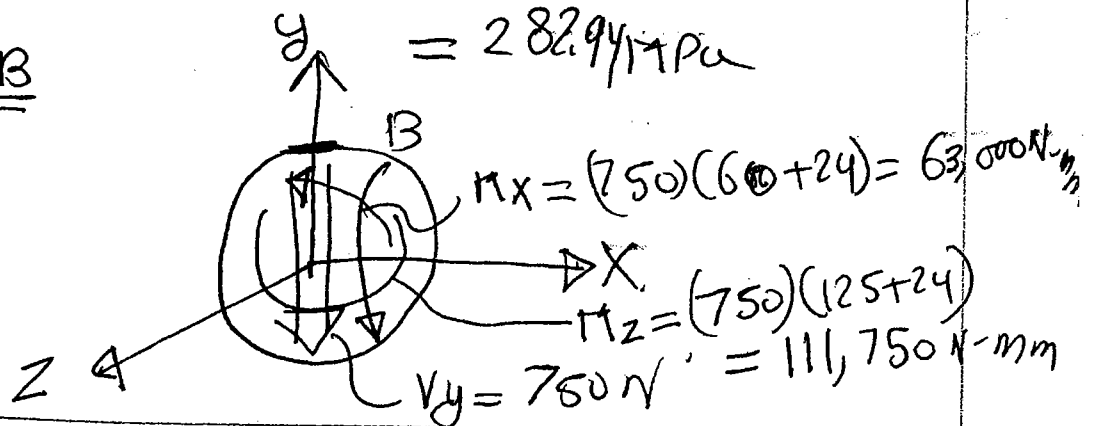
$M_x = T = (750)(60) = 45,000\text{ N-mm}$

$M_z = (750)(125) = 93,750\text{ N-mm}$

$\tau = \frac{T R}{J} = \frac{2T}{\pi R^3} = \frac{2(45,000)}{\pi(7.5)^3} = 67.91\text{ MPa}$

$\sigma = \frac{M_z R}{\frac{1}{4}\pi R^3} = \frac{4M_z}{\pi R^3} = \frac{4(93,750)}{\pi(7.5)^3}$

POINT B



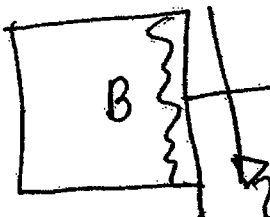
$= 282.94\text{ MPa}$

$M_x = (750)(60 + 24) = 63,000\text{ N-mm}$

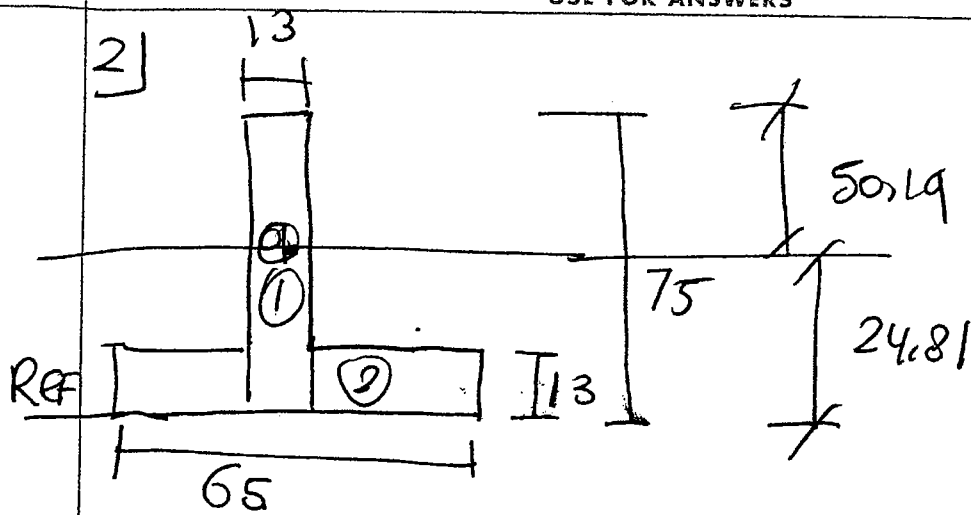
$M_z = (750)(125 + 24) = 111,750\text{ N-mm}$

$V_y = 750\text{ N}$




$$\sigma = \frac{M \times R}{\frac{\pi}{4} R^4} = \frac{4M}{\pi R^3} = \frac{4(63,000)}{\pi (7.5)^3} = 140 \text{ MPa}$$
$$\tau = \frac{M \times R}{\frac{\pi}{2} R^4} = \frac{2M}{\pi R^3} = \frac{2(11,750)}{\pi (7.5)^3} = 68.68 \text{ MPa}$$

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$$\bar{y} = \frac{(75)(13)(75/2) + (13)(65-13)(13/2)}{(75)(13) + (13)(65-13)} = 24.81 \text{ mm}$$

$$y_{\text{TOP}} = 75 - 24.81 = 50.19 \text{ mm}$$

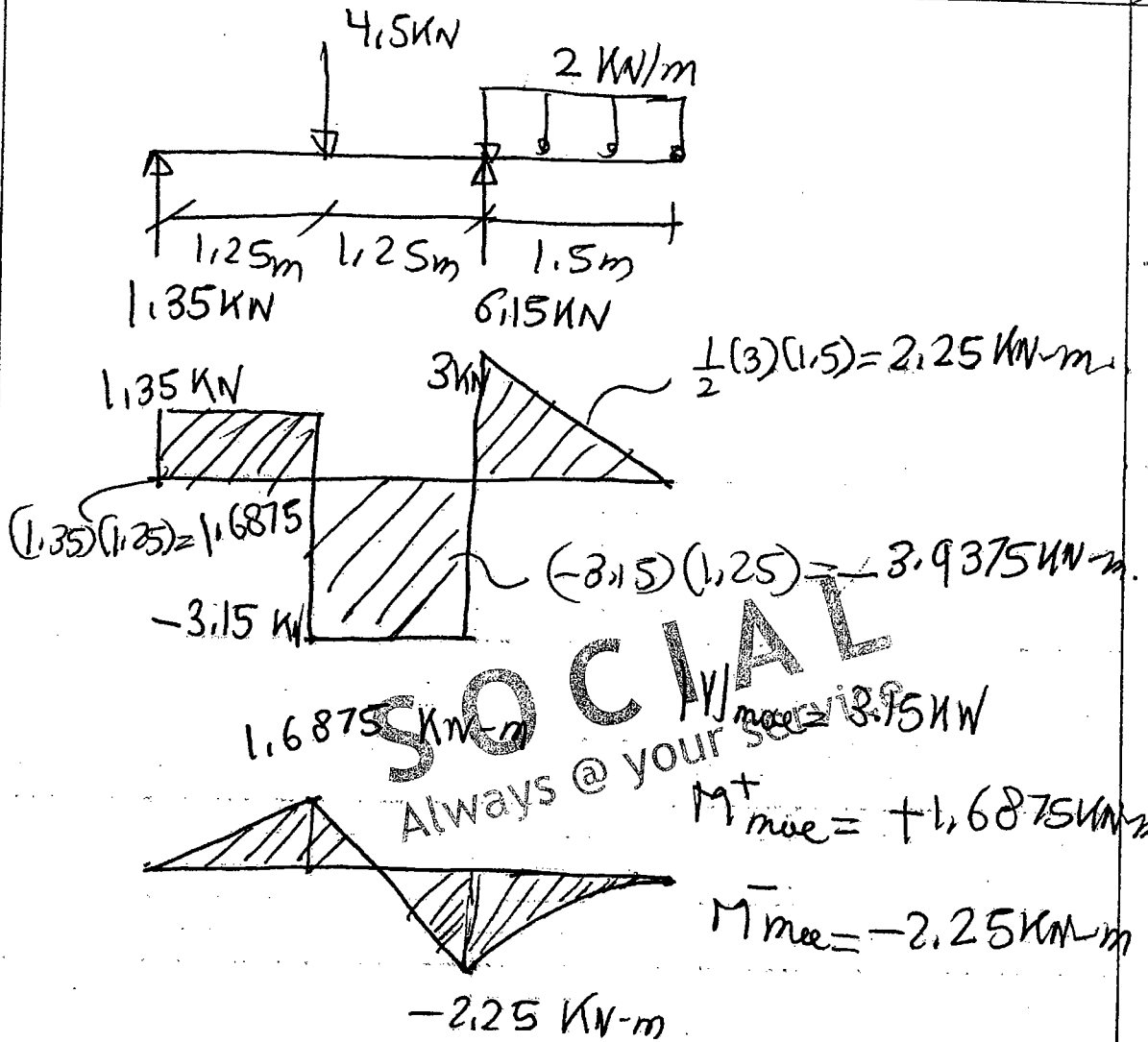
$$I = \frac{1}{12}(13)(75)^3 + (13)(75)\left(\frac{75}{2} - 24.81\right)^2 + \frac{1}{12}(65-13)(13)^3 + (65-13)(13)\left(13/2 - 24.81\right)^2 = 850,194,90 \text{ mm}^4$$

$$I_m = 13 \text{ mm}$$

$$Q_m = (50.19)(13)\left(\frac{50.19}{2}\right) = 16,373.73 \text{ mm}^3$$

$$R_R = \left\{ (4.5)(1.25) + (2)(1.5) \left[ 2.5 + (1.5/2) \right] \right\} / 2.5 = 6.15 \text{ kN}$$

$$V_L = \left[ (4.5)(1.25) - (2)(1.5)(1.5/2) \right] / 2.5 = 1.35 \text{ kN}$$



$$\tau_m = \frac{V_{\text{max}} Q_m}{I \epsilon_m} = \frac{(3.15 \times 10^3)(16,373.73)}{(850,194.90)(13)} = 4.67 \text{ MPa}$$

$$\sigma_{\text{TOP}} = -\frac{M y_{\text{TOP}}}{I} = -\frac{(1.6875 \times 10^6)(50.19)}{850,194.90} = -99.62 \text{ MPa}$$

$$\sigma_{\text{BOT}} = -\frac{M y_{\text{BOT}}}{I} = -\frac{(1.6875 \times 10^6)(-24.81)}{850,194.90} = +49.24 \text{ MPa}$$

$$\sigma_{\text{TOP}} = -\frac{(-2.25 \times 10^6)(50.19)}{850,194.90} = +132.83 \text{ MPa} = \sigma_{\text{TEN}}^{\text{MAX}}$$

$$\sigma_{\text{BOT}} = -\frac{(-2.25 \times 10^6)(-24.81)}{850,194.90} = -65.66 \text{ MPa}$$



$$b) \sigma_x = -27 \text{ MPa}, \sigma_y = +5,5 \text{ MPa}, \tau_{xy} = -10,5 \text{ MPa}$$

$$\tau_{\text{ave}} = \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + (\tau_{xy})^2}$$

$$\tau_{\text{ave}} = \sqrt{\left(\frac{-27 - 5,5}{2}\right)^2 + (-10,5)^2} = 19,35 \text{ MPa}$$

$$\sigma_{\text{ave}} = \frac{\sigma_x + \sigma_y}{2} = \frac{-27 + 5,5}{2} = -10,75 \text{ MPa}$$

$$\sigma_{\text{max, min}} = \sigma_{\text{ave}} \pm \tau_{\text{ave}}$$

$$= -10,75 \pm 19,35$$

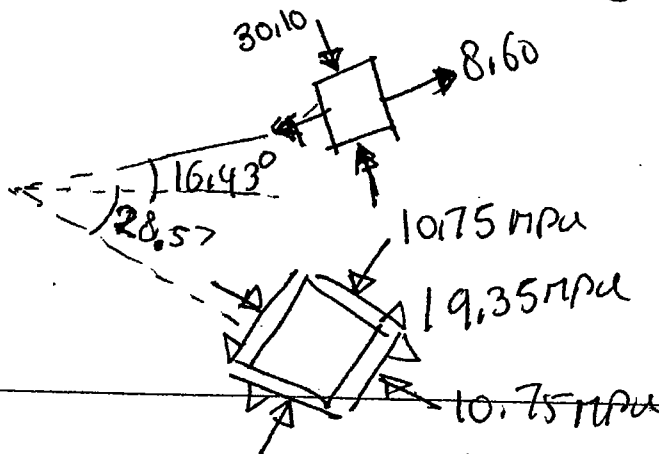
$$= 8,60 \text{ MPa} \text{ and } -30,10 \text{ MPa}$$

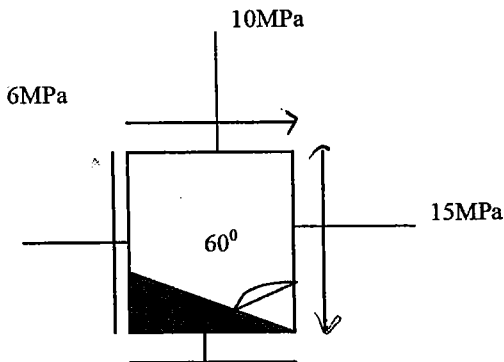
$$\sigma_p = \frac{1}{2} \left( \text{TAN}^{-1} \left[ \frac{2\tau_{xy}}{\sigma_x - \sigma_y} \right] \right)$$

$$= \frac{1}{2} \left\{ \text{TAN}^{-1} \left[ \frac{2(-10,50)}{-27 - 5,5} \right] \right\} = 16,43^\circ$$

$$\sigma_s = \frac{1}{2} \left\{ \text{TAN}^{-1} \left[ \frac{\sigma_x - \sigma_y}{-2\tau_{xy}} \right] \right\}$$

$$= \frac{1}{2} \left\{ \text{TAN}^{-1} \left[ \frac{-27 - 5,5}{-2(-10,50)} \right] \right\} = -28,57^\circ$$

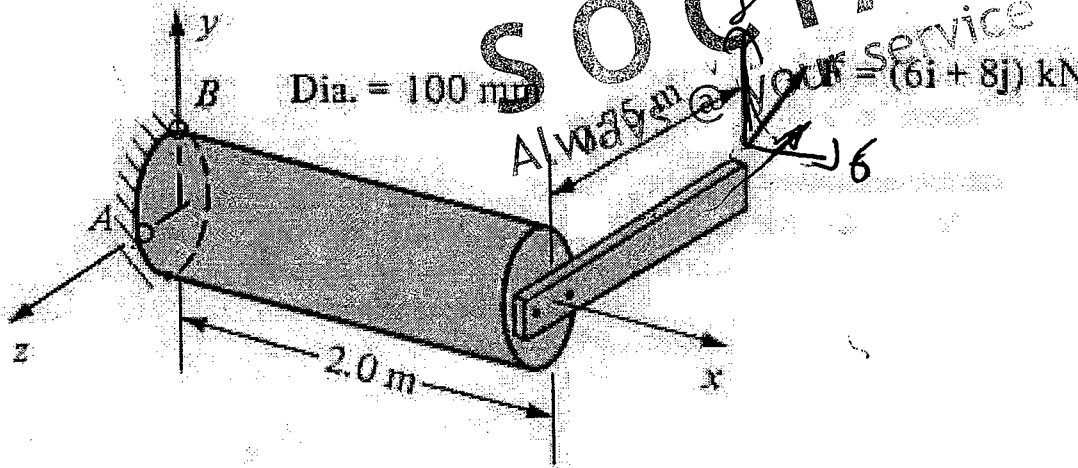




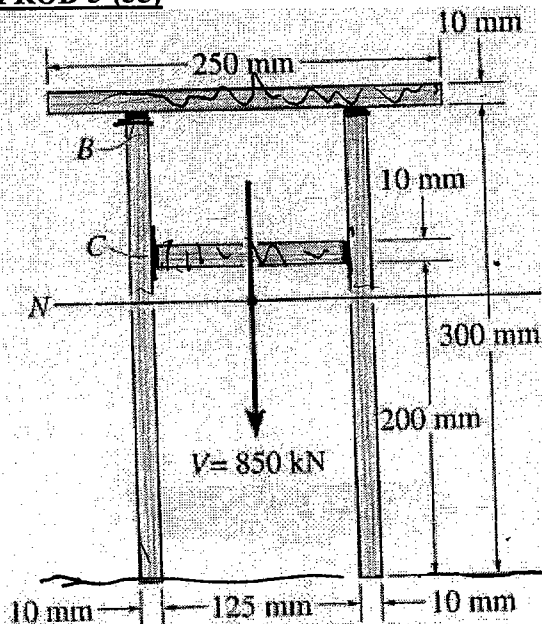
For the stress state shown to the right: a) Determine the normal and shearing stresses for the shaded area using the method of equilibrium; b) Determine the principal stresses and the maximum shearing stress.

**PROB-2-(40)**

A circular hollow shaft 100 mm in outer diameter and wall thickness of 10 mm is fixed at one end and loaded as shown below. Compute the state of stress at points A and B located at the fixed end. Present your analysis and the state of stress acting on an element.

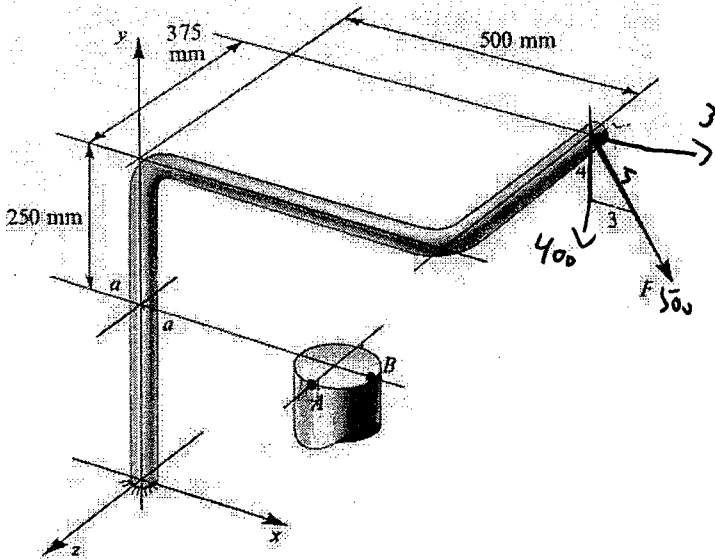


**PROB-3-(35)**



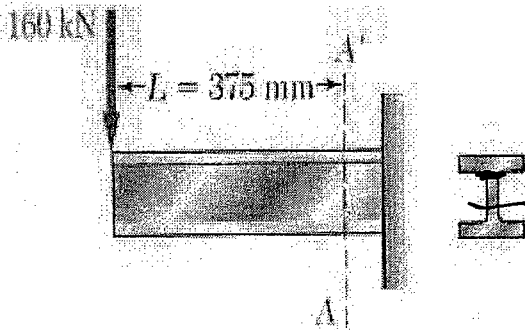
The beam is constructed from four boards glued together as shown to the left. If it is subjected to a shear of  $V = 850$  kN, determine a) the shear flow at B and C that must be resisted by the glue; b) the maximum shearing stress in the composite section.

**PROB-1-(35)**



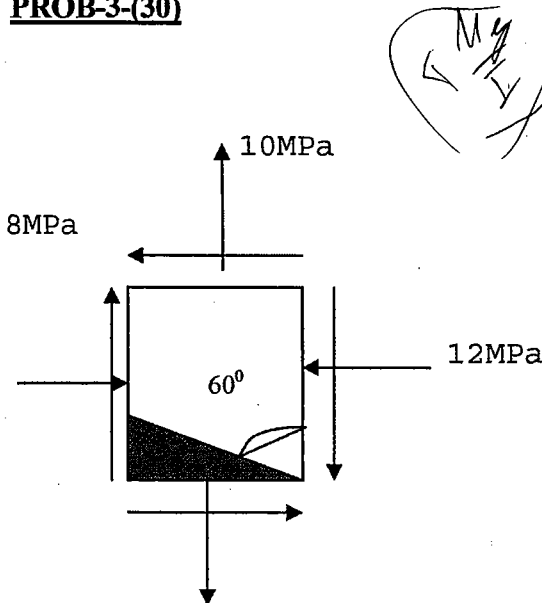
A 30 mm diameter rod is subjected at its free end to an inclined force  $F = 500$  N as in the figure. (The force  $F$  in plan view acts in the direction of the  $x$  axis and has an  $x$  and  $y$  component.) Determine the magnitude and directions of the stresses due to  $F$  on the elements  $A$  and  $B$  at section  $a-a$ . Show the results on elements clearly related to the points on the rod.

**PROB-2- (30)**



A 160-kN force is applied as shown at the end of a W200 x 52 rolled steel beam. Determine whether the normal stresses in the beam satisfy a design specification that they should be equal to or less than 155 MPa at section  $A-A$  by looking at (a) the maximum value of the normal stress in the beam, and (b) the maximum value of the principal stress at the junction of the flange and the web.

**PROB-3-(30)**

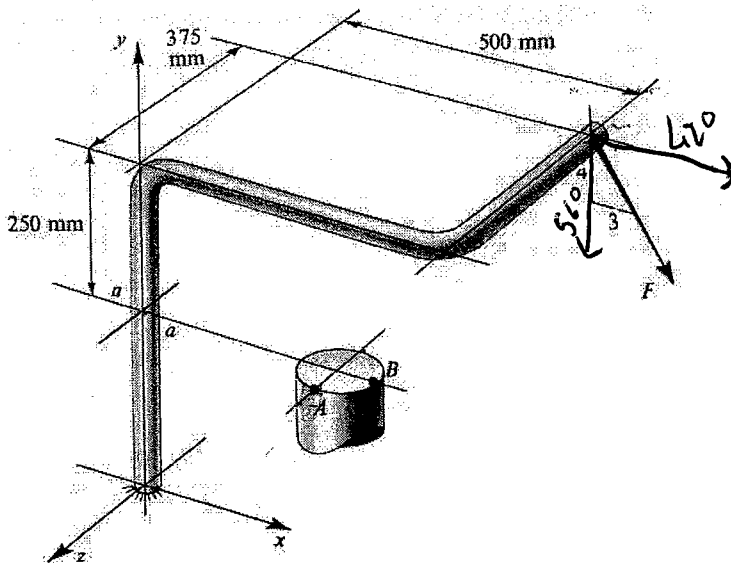


For the stress state shown to the left, determine: a) the normal and shearing stresses for the shaded area using the method of equilibrium; b) The principal stresses and maximum shearing stress.





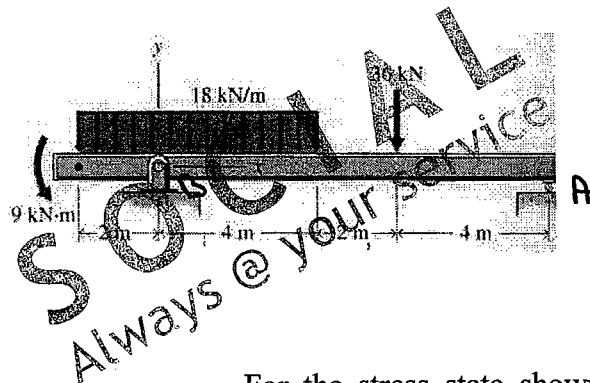
**PROB-1-(35)**



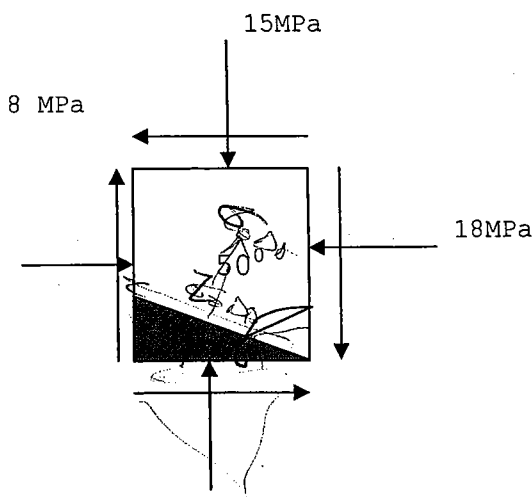
A 50 mm diameter rod is subjected at its free end to an inclined force  $F = 700\text{ N}$  as in the figure. (The force  $F$  in plan view acts in the direction of the  $x$  axis and has an  $x$  and  $y$  component.) Determine the magnitude and directions of the stresses due to  $F$  on the elements  $A$  and  $B$  at section  $a-a$ . Show the results on elements clearly related to the points on the rod.

**PROB-2-(35)**

For the beam shown below, draw the moment and shear diagrams.



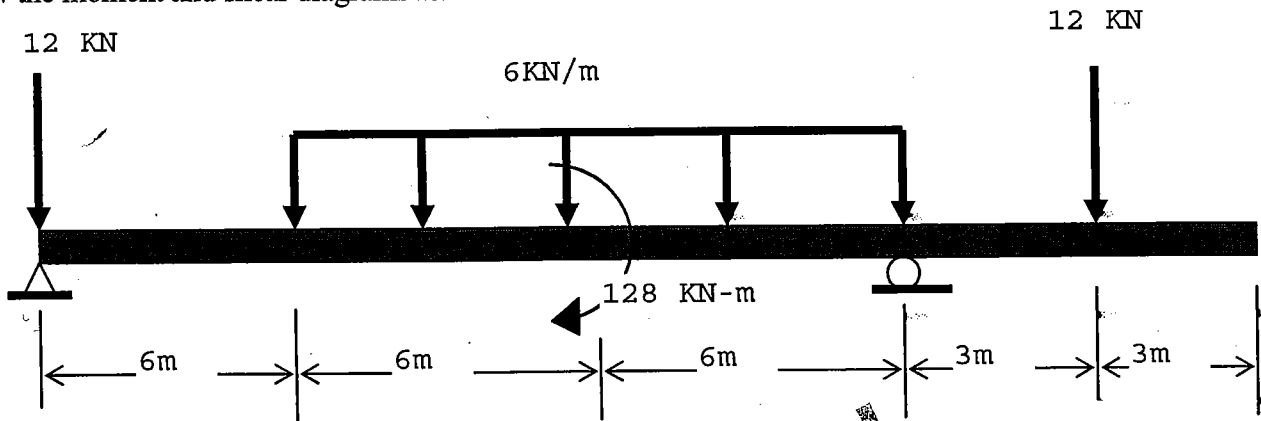
**PROB-3-(30)**



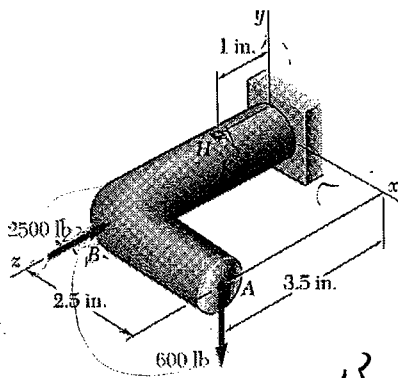
For the stress state shown to the left, determine: a) the normal and shearing stresses for the shaded area using the method of equilibrium; b) The principal stresses and maximum shearing stress.

**PROB-1-(35)**

Draw the moment and shear diagrams for the beam shown below.



**PROB-2- (35)**



Forces are applied at points A and B of the solid cast-iron bracket shown. Knowing that the bracket has a diameter of 0.8 in., Determine and draw the stress element at point H.

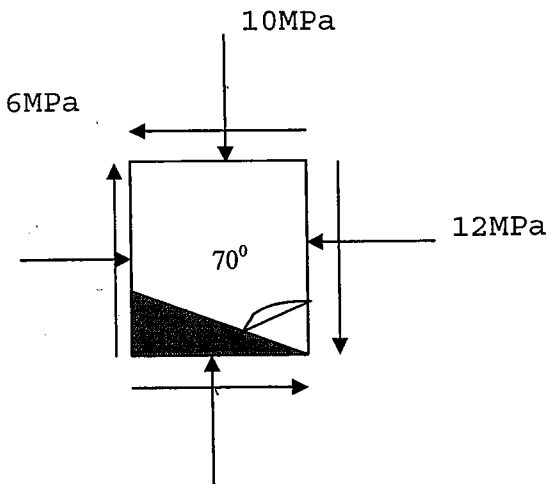
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**PROB-3-(30)**

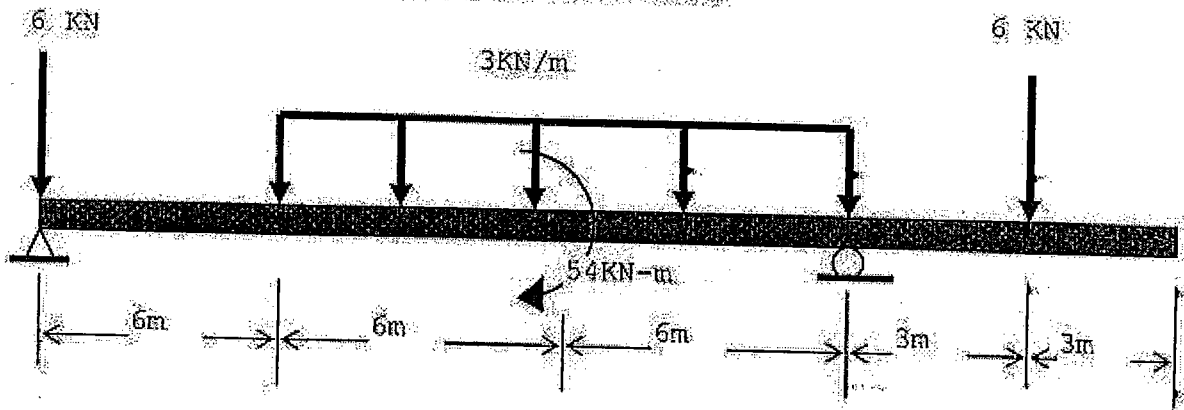
*Don't miss*

For the stress state shown to the left, determine: a) the normal and shearing stresses for the shaded area using the method of equilibrium; b) The principal stresses and maximum shearing stress.

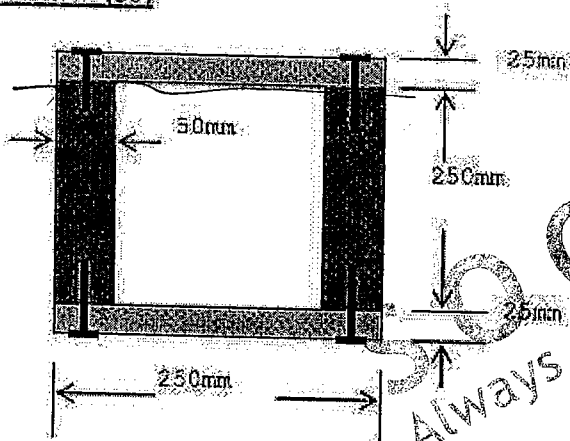


**PROB-1-(40)**

Draw the moment and shear diagrams for the beam shown below.



**PROB-2-(30)**

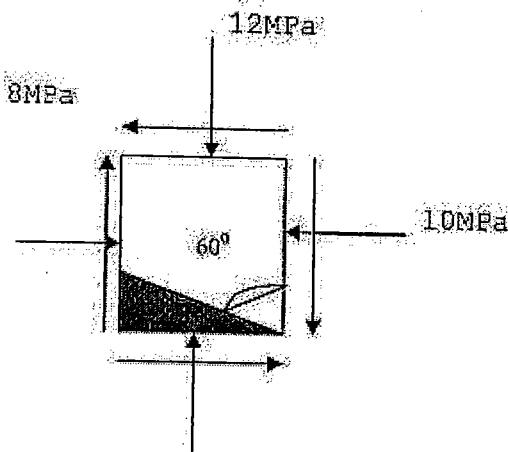


A wood beam is constructed of two members 50 mm X 250mm in a cross section that are attached by two 25mm X 250mm boards as shown in figure. The boards are nailed to the beams at a longitudinal spacing of 100 mm. The allowable force per nail is 1300 N. a) Determine the maximum vertical shear force that could be handle by the section. b) Determine the maximum shearing stress if the vertical shear force is 10 kN.

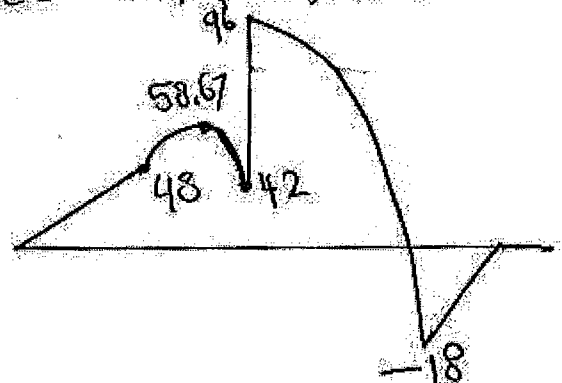
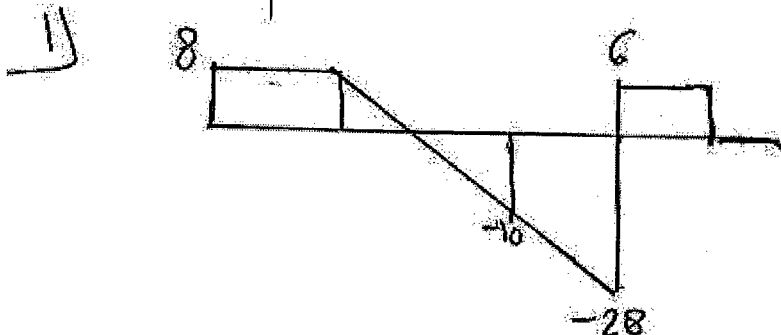
a)  $V = 11.10 \text{ kN}$   
 b)  $\tau_m = 0.45 \text{ MPa}$

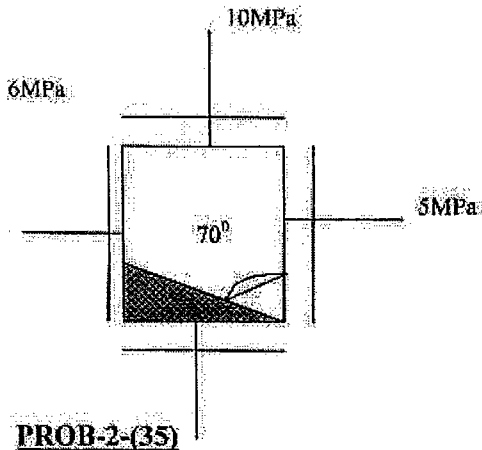
**PROB-3-(30)**

For the stress state shown to the left, determine: a) the normal and shearing stresses for the shaded area using the method of equilibrium; b) The principal stresses and maximum shearing stress.



a)  $\tau_{\theta} = 3.13 \text{ MPa}$   
 $\sigma_{\theta} = 18.43 \text{ MPa}$   
 b)  $\tau_{max} = 8.06 \text{ MPa}$   
 $\sigma_{min} = -2.94 \text{ MPa}, \sigma_{max} = 19.66 \text{ MPa}$





For the stress state shown to the right: a) Determine the normal and shearing stresses for the shaded area using the method of equilibrium; b) Determine the principal stresses and the maximum shearing stress.

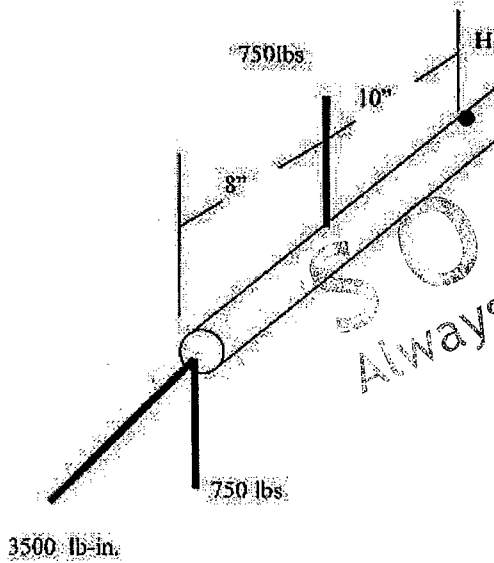
$$\tau_{\theta} = -9.42 \text{ MPa}$$

$$\sigma_{\theta} = 4.39 \text{ MPa}$$

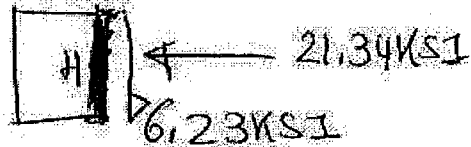
$$\tau_{max} = 9.60 \text{ MPa}$$

$$\sigma_{max, min} = 12.10; -7.10 \text{ MPa}$$

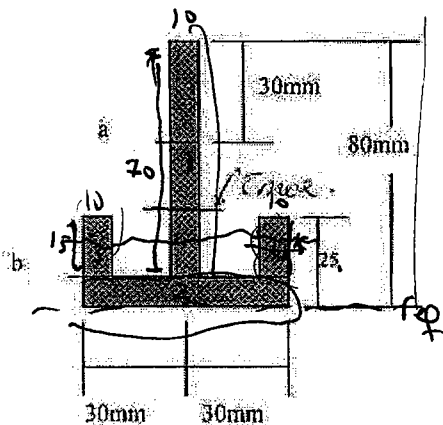
PROB-2-(35)



The axle of a small truck is acted upon by the forces and couple shown. Knowing that the diameter of the axle is 1.42 inches, determine the stress state at point H located on the top of the axle.



PROB-3-(40)



The cross section of the beam shown to the right is 10 mm thick and is acted upon by a shear force of 20 kN. Determine: a) The shearing stress at point a; b) The shearing stress at point b; and c) The maximum shearing stress in the beam.

$$\tau_a = 28.91 \text{ MPa}$$

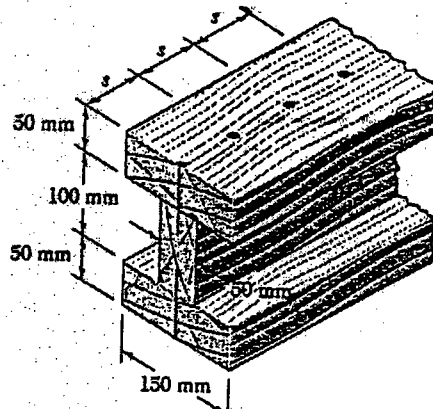
$$\tau_b = 9.53 \text{ MPa}$$

$$\tau_{max} = 12.17 \text{ MPa}$$

$$\tau_{max} = 36.51 \text{ MPa} \leftarrow \text{CONTROLS}$$

PROB-1-(30)

Three boards, each 50 mm thick, are nailed together to form a beam that is subjected to a 1200 n vertical shear. Knowing that the allowable shearing force in each nail is 300 N, determine the largest permissible spacing  $s$  between nails.

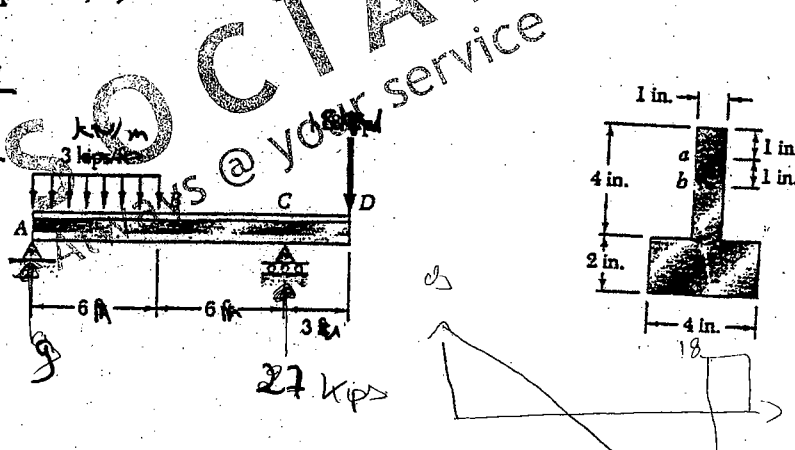


$S = 40.74 \text{ mm}$

PROB-2-(35)

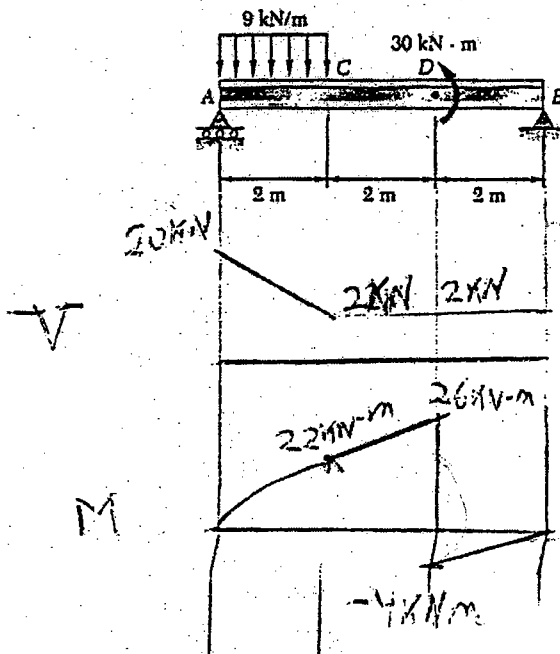
For the beam and loading shown, consider a section at point B of the beam and determine i) the shearing stress at point a, ii) the shearing stress at point b, iii) the maximum shearing stress.

$\tau_a = 0.984 \text{ ksi}$   
 $\tau_b = 1.6875 \text{ ksi}$   
 $\tau_c = 2.25 \text{ ksi}$



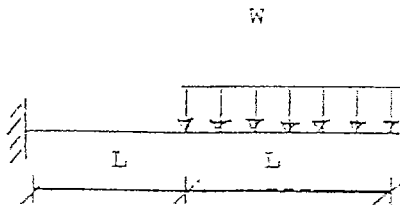
PROB-3-(35)

Draw the moment and shear diagrams for the beam shown below.



PROB-1

For the beam and loading shown below, determine the equation of the deflection.



$0 \leq x \leq L$

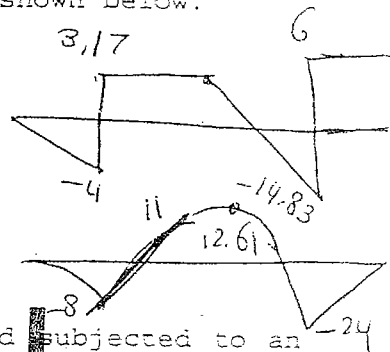
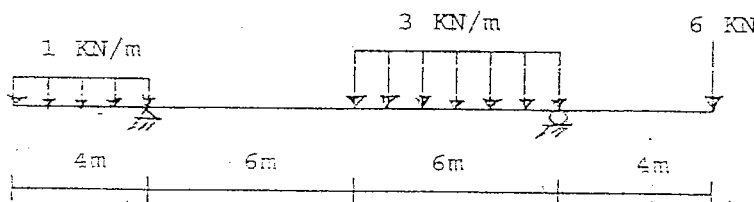
$V = wL, \quad \pi = wLx - \frac{3}{2}wL^2$

$L \leq x \leq 2L \quad y = \frac{1}{EI} \left( \frac{wLx^3}{6} - \frac{3wL^2x^2}{4} \right)$

$y = \frac{1}{EI} \left[ -wL^2x^2 - \frac{wx^4}{24} + \frac{wx^3L}{3} + \frac{wL^3x}{3} - \frac{wL^4}{24} \right]$

PROB-2

Draw the moment and shear diagrams for the beam shown below.



PROB-3

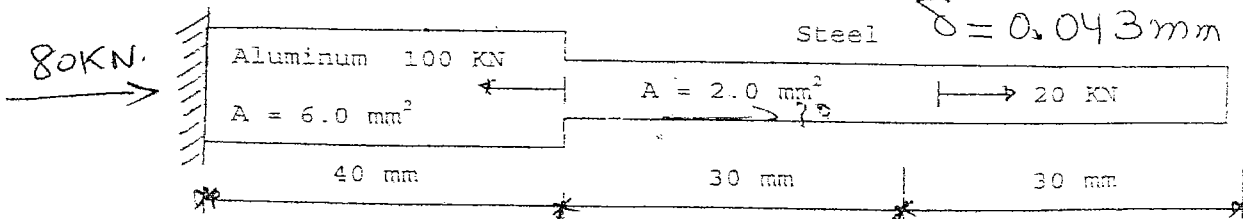
cho: 1+2

Find the required cross sectional area of a rod subjected to an axial load of 35 kN, if the stress is not to exceed 200 MPa and the elongation is not exceed 0.10 mm. The rod is 1 m long and is made of steel ( $E = 30 \times 10^6 \text{ MPa}$ ).

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PROB-4

The bar shown below is made from aluminum ( $E = 10 \times 10^6 \text{ MPa}$ ) and steel ( $E = 30 \times 10^6 \text{ MPa}$ ) and is loaded with two axial loads. Determine the net movement of the free end.



$\delta = 0.043 \text{ mm}$

PROB-5

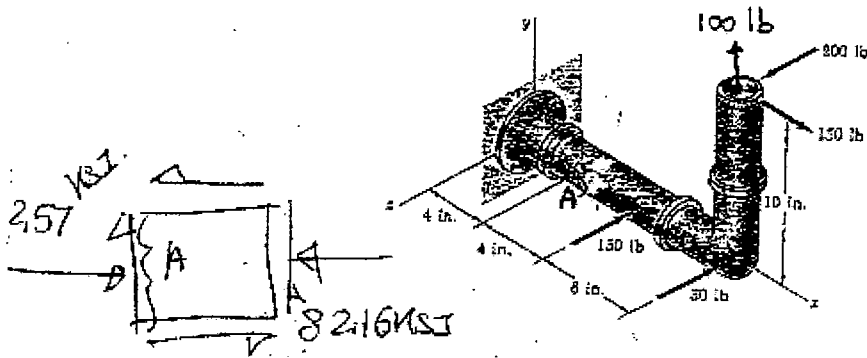
The cross section shown on next page is subjected to a constant shear of 750 N. Compute the required spacing of the nails along the beam, if the allowable shear force is 75 N/nail. Given  $I_c = 892 \text{ mm}^4$ .

PROB-9

A 12 m long by 12.5 mm diameter steel rod is subjected to an axial tensile load of 25 kN. The total elongation is 0.07 mm. Calculate the: a) axial stress ; b) axial strain.

PROB-10  $\sigma = 203.72 \text{ MPa}$   $\epsilon = 0.583 \times 10^{-5}$

The solid shaft shown below is 0.5" in diameter and is acted upon by the forces as shown. Determine the stress state at point A and draw the stress element. Solve the problem by looking at point A from the left hand side.



EQUATIONS:

$\delta = \delta/L$  ;  $\sigma = P/A$  ;  $\sigma = E\epsilon$  ;  $\delta = \sum (P_i L_i) / (A_i E_i)$  ;  $\tau = (VQ) / (It)$  ;

$q = (VQ) / I$  ;  $\sigma = -(My) / I$  ;  $F_n = q_s$  ;  $\tau = (Tr) / J$  ;  $A = bh$  ;  $A =$

$A = \pi R^2$  ;  $I = bh^3 / 12$  ;  $J = \pi / 2 (R_o^4 - R_i^4)$  ;  $I = \pi / 4 (R_o^4 - R_i^4)$  ;

$\epsilon = \alpha \Delta T$  ;  $Q = \sum A_i y_i$  ;  $\bar{y} = \sum A_i y_i / (\sum A_i)$

$\phi = \sum (T_i L_i) / (J_i G_i)$  ;  $I_c = \sum (I_{c1} + A_i d_i^2)$  ;  $dV/dx = -w(x)$  ;

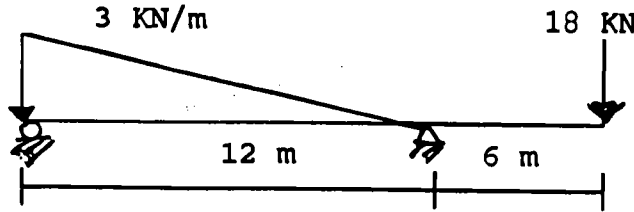
$dM/dx = V$  ;  $d^2 y / dx^2 = M / EI$

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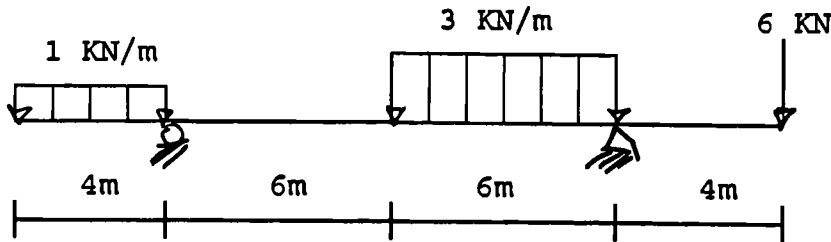
**PROB-1**

For the beam shown below determine the equation of deflection



**PROB-2**

Draw the moment and shear diagrams for the beam shown below.

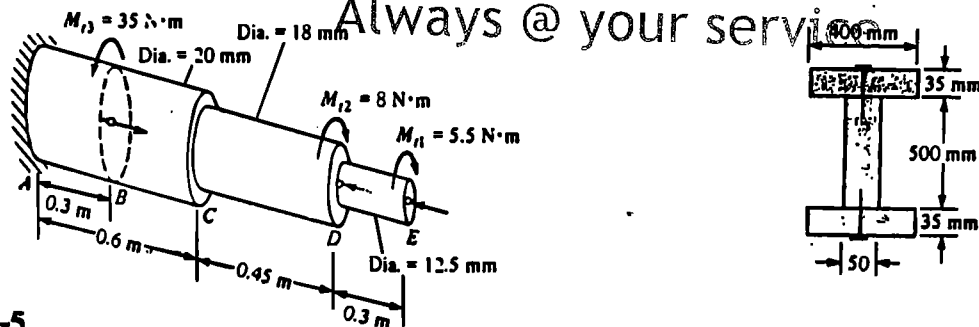


**PROB-3**

Find the required cross sectional area of a rod subjected to an axial load of 35 kN, if the stress is not to exceed 200 MPa and the elongation is not exceed 0.10 mm. The rod is 1.5 m long and is made of steel ( $E = 30E06$  MPa).

**PROB-4**

The shaft shown below is made from aluminum ( $G = 85$  GPa). Determine the rotation of the free end, and the maximum shearing stress in the shaft.

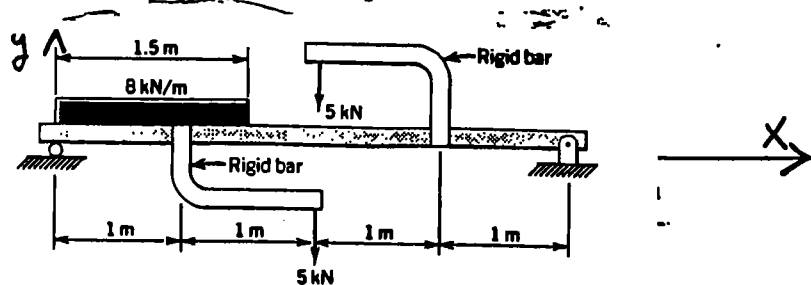


**PROB-5**

The I cross section shown above is subjected to a constant shear of 8 kN. Compute the required spacing of the nails along the beam, if the allowable shear force is 800 N/nail.

**PROB-6**

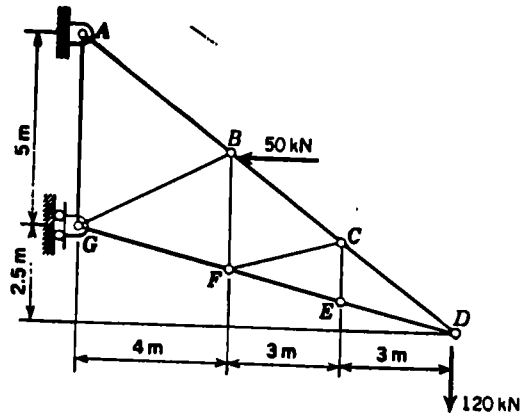
Write the moment and shear equations for the beam shown below.





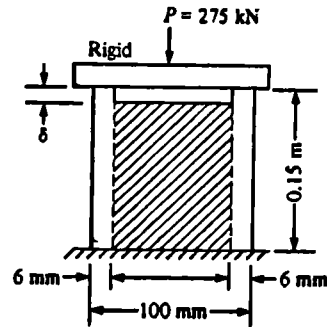
**PROB-7**

Determine the stress in members GF of the truss shown below. Given:  $A_{GF} = 4500 \text{ mm}^2$ .



**PROB-8**

A square steel ( $E = 200 \text{ GPa}$ ) container with outside dimensions 100 mm by 100 mm and sides of 6 mm thickness. The container is filled with a material of  $E = 30 \text{ GPa}$  and leaving a gap of 0.025 mm at the top of the container as shown below. A force of 275 kN is applied on the container, determine the stress on the material inside the container.

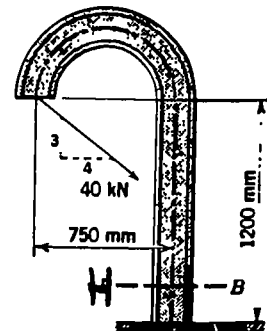


**PROB-9**

A 12 m long by 12.5 mm diameter steel rod is subjected to an axial tensile load of 25 kN. The total elongation is 0.07 mm. Calculate the: a) axial stress ; b) axial strain.

**PROB-10**

The solid rod shown below is 30 mm in diameter and is acted upon by the forces as shown. Determine the stress state at point H and draw the stress element. Solve the problem by looking at point H from the top side.

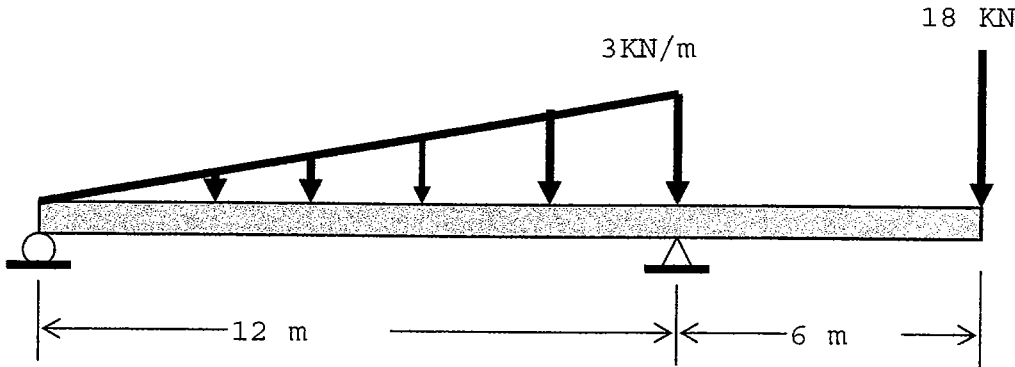


**EQUATIONS:**

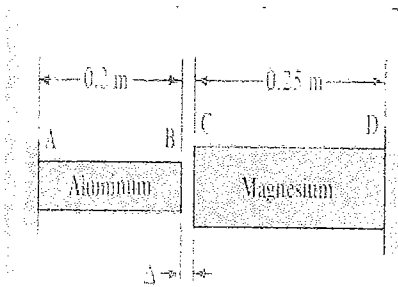
$$\begin{aligned} \epsilon &= \delta/L ; \sigma = P/A ; \sigma = E\epsilon ; \delta = \sum (P_i L_i) / (A_i E_i) ; \tau = (VQ) / (It) ; \\ q &= (VQ) / I ; \sigma = -(My) / I ; F_n = qs ; \tau = (Tr) / J ; A = bh ; A = \\ &= bh/2 ; A = \pi R^2 ; I = bh^3 / 12 ; J = \pi / 2 (R_o^4 - R_i^4) ; I = \pi / 4 (R_o^4 - R_i^4) \\ &; \epsilon = \alpha \Delta T ; Q = \sum A_i d_i ; d_i = |Y_i - Y_c| ; Y_c = (\sum A_i Y_i) / (\sum A_i) \\ &; \phi = \sum (T_i L_i) / (J_i G_i) ; I_c = \sum (I_{oi} + A_i d_i^2) ; dV/dx = -w(x) ; \\ &dM/dx = V ; d^2y/dx^2 = M/EI \end{aligned}$$

**PROB-1**

For the beam shown below, draw the moment and shear diagrams.



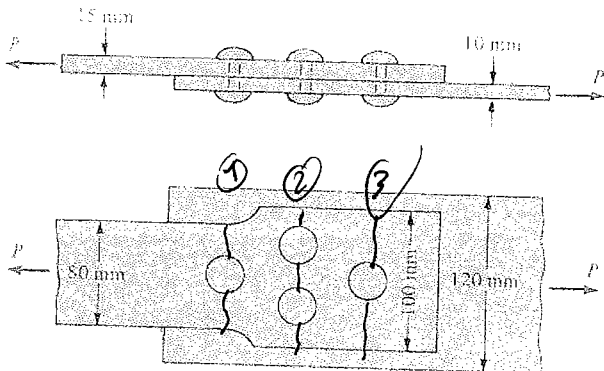
**PROB-2**



At 20°C there is a gap  $\Delta = 0.4$  mm between the ends of the aluminum and magnesium bars shown in Figure. Use  $E_a = 70$  GPa,  $\alpha_a = 23 \times 10^{-6}/^\circ\text{C}$ ,  $A_a = 500$  mm<sup>2</sup>,  $E_m = 45$  GPa,  $\alpha_m = 26 \times 10^{-6}/^\circ\text{C}$  and  $A_m = 1200$  mm<sup>2</sup>. Determine (a) the compressive stress in each rod when the temperature rises to 120°C and (b) the change in length of the magnesium bar.

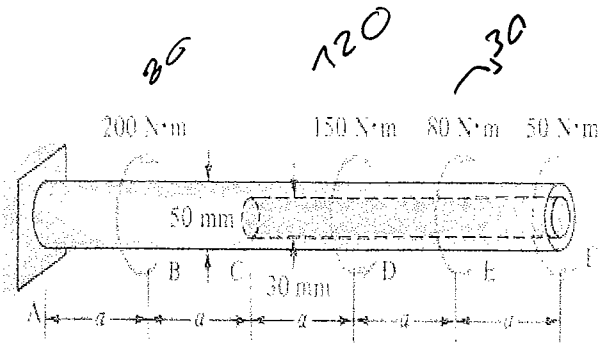
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**PROB-3**



Two plates are joined by four rivets of 20-mm diameter, as shown in Figure. Determine the maximum load  $P$  if the shearing, tensile, and bearing stresses are limited to 80, 100, and 140 MPa, respectively. Assume that the load is equally divided among the rivets.

**PROB-4**



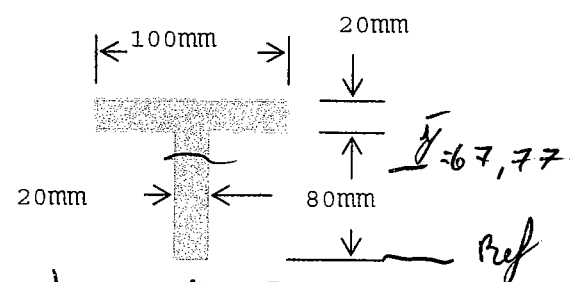
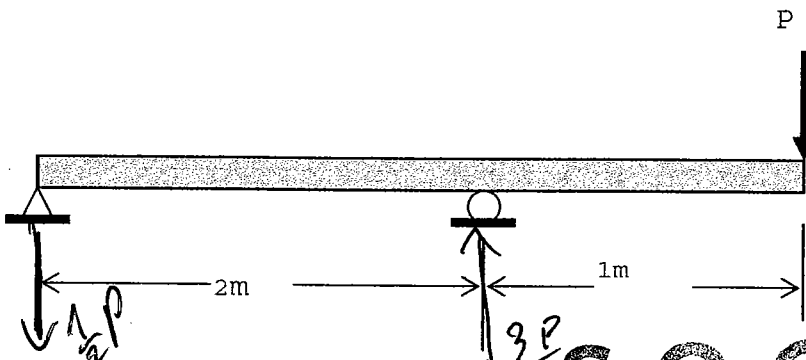
Determine: a) the largest shearing stress in the shaft. b) the angle of rotation in degrees at F. Given  $G = 80 \text{ GPa}$

$$\tau_{FA} = \frac{T}{J} \cdot r = \frac{200}{\frac{\pi}{32} (50^4)} \cdot 25 = 32,628,463$$

$$\tau_{AE} = \dots$$

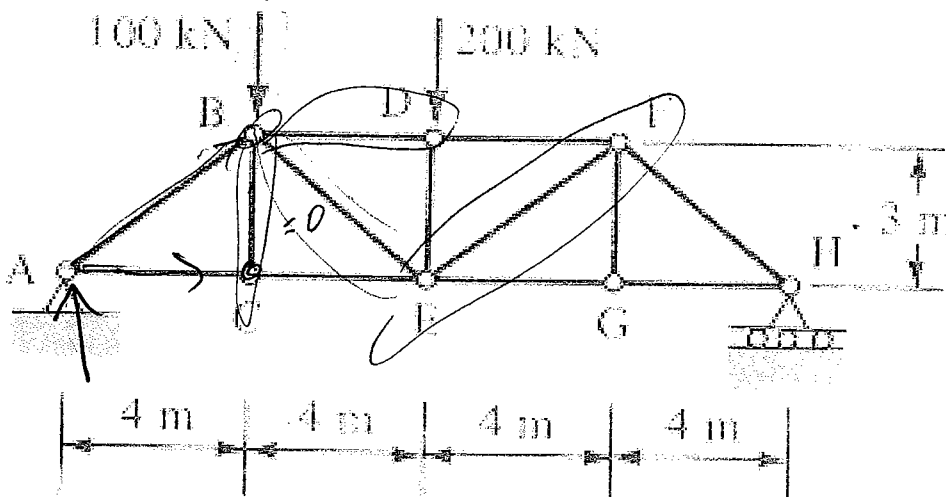
**PROB-5-**

Determine the value of load P so that the maximum allowable stresses does not exceed 40 M Pa in tension, 70 M Pa in compression, and 12 M Pa in shear.



**PROB-6-**

Determine the stress in members FE, BD, and BC of the truss shown below. Given  $A_c = 5000 \text{ mm}^2$ .



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$P = 16,42 \text{ KN}$

$\sigma = -\frac{P}{A}$

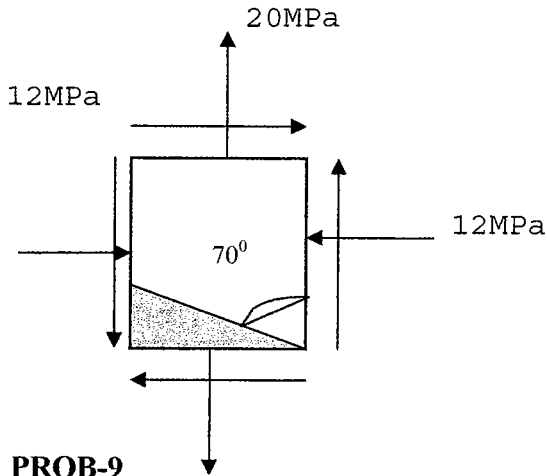
$4,467$   
 $3,712 \text{ KN}$

**PROB-7-**

A 2 inch diameter and 4 inch long solid cylinder is subjected to uniform axial stress of 7.2 Ksi. Use  $E = 30 \times 10^3 \text{ Ksi}$  and  $\nu = \frac{1}{3}$ . Calculate: a) the change in length, b) the change in diameter.

**PROB-8**

For the stress state shown to the left, determine the normal and shearing stresses for the shaded area using the method of equilibrium.



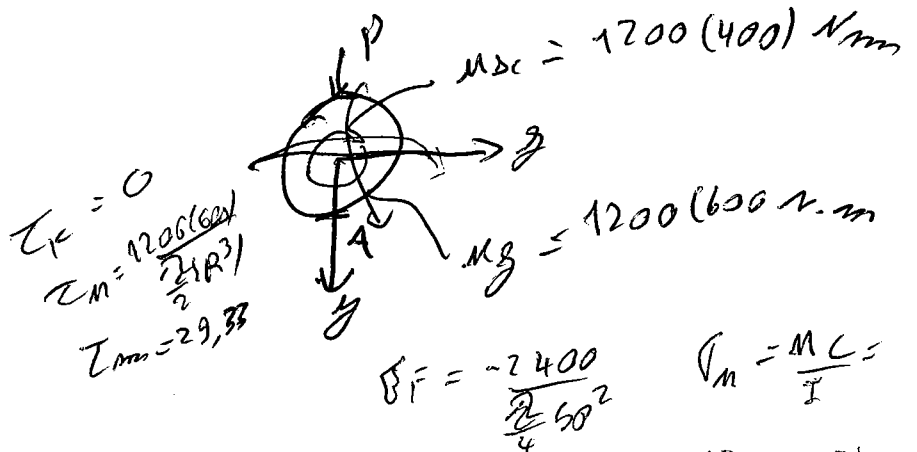
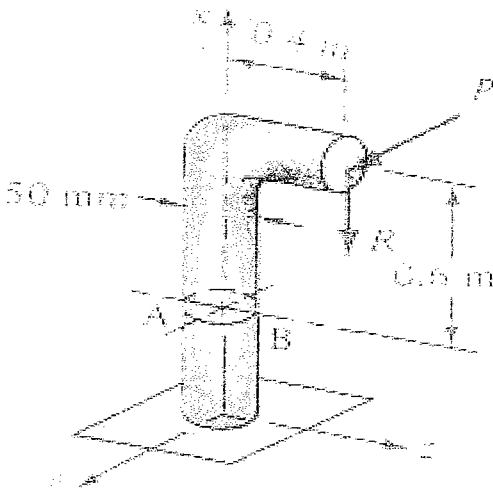
**PROB-9**

Draw the moment and shear diagrams for the beam shown below.



**PROB-10**

Loads  $P = 1200 \text{ N}$  and  $R = 2400 \text{ N}$  are applied at the free end of the 50 mm diameter post shown. Determine the stress state at point A and draw the stress element. Solve the problem by looking at point A from the top side



**EQUATIONS:**

$$\epsilon = \delta/L ; \sigma = P/A ; \sigma = E\epsilon ; \delta = \sum (P_i L_i) / (A_i E_i) ; \tau = (VQ) / (It) ; y = \frac{4R}{3\pi} ; I = \frac{\pi R^4}{4} ;$$

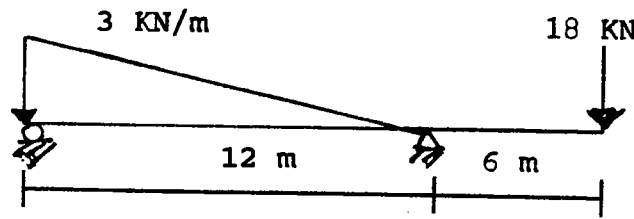
$$q = (VQ) / I ; \sigma = -(My) / I ; F_n = qs ; \tau = (Tr) / J ; A = bh ; A = bh/2 ; A = \pi R^2 ;$$

$$I = bh^3/12 ; J = \pi/2 (R_o^4 - R_i^4) ; I = \pi/4 (R_o^4 - R_i^4) ; \epsilon = \alpha \Delta T ; Q = \sum A_i d_i ;$$

$$d_i = |y_i - y_c| ; y_c = (\sum A_i y_i) / (\sum A_i) ; \phi = \sum (T_i L_i) / (J_i G_i) ;$$

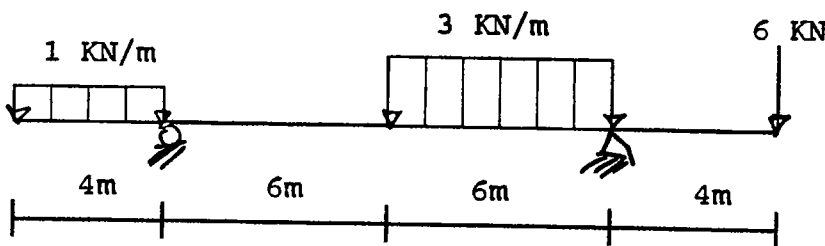
**PROB-1**

For the beam shown below determine the equation of deflection



**PROB-2**

Draw the moment and shear diagrams for the beam shown below.



*I<sub>y</sub> = 374 2222, 4*  
*t = 20*  

$$r = \frac{VQ}{I_t}$$

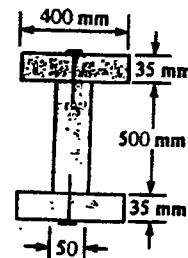
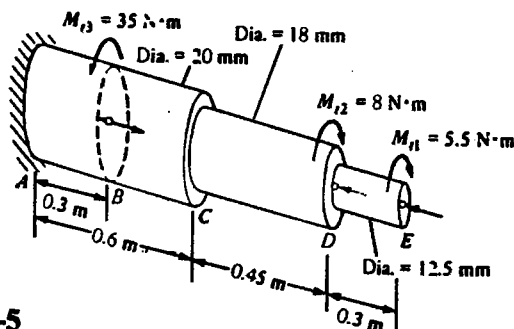
**PROB-3**

Find the required cross sectional area of a rod subjected to an axial load of 35 kN, if the stress is not to exceed 200 MPa and the elongation is not exceed 0.10 mm. The rod is 1.5 m long and is made of steel ( $E = 30E06$  MPa).

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**PROB-4**

The shaft shown below is made from aluminum ( $G = 85$  GPa) . Determine the rotation of the free end, and the maximum shearing stress in the shaft.

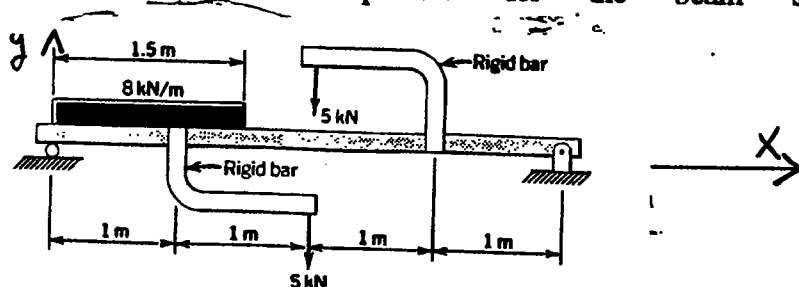


**PROB-5**

The I cross section shown above is subjected to a constant shear of 8 kN. Compute the required spacing of the nails along the beam, if the allowable shear force is 800 N/nail.

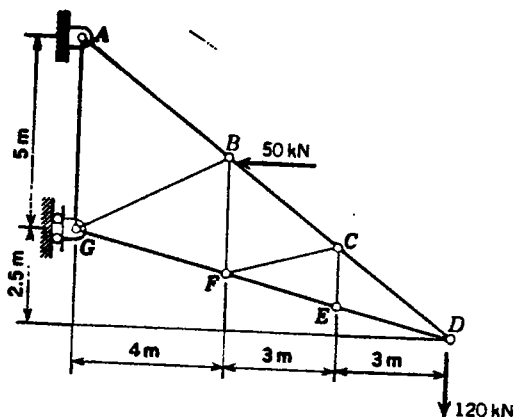
**PROB-6**

Write the moment and shear equations for the beam shown below.



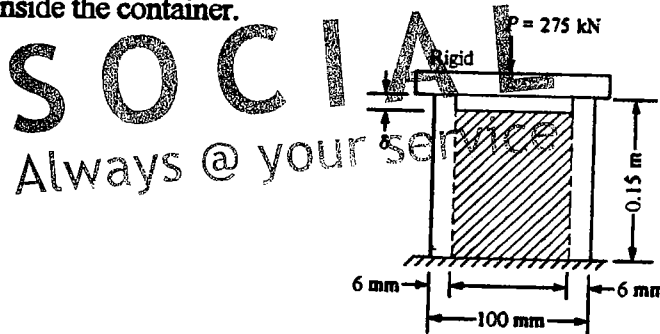
**PROB-7**

Determine the stress in members GF of the truss shown below. Given:  $A_{GF} = 4500 \text{ mm}^2$ .



**PROB-8**

A square steel ( $E = 200 \text{ GPa}$ ) container with outside dimensions 100 mm by 100 mm and sides of 6 mm thickness. The container is filled with a material of  $E = 30 \text{ GPa}$  and leaving a gap of 0.025 mm at the top of the container as shown below. A force of 275 kN is applied on the container, determine the stress on the material inside the container.

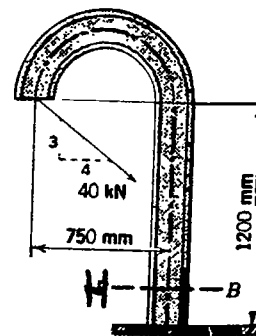


**PROB-9**

A 12 m long by 12.5 mm diameter steel rod is subjected to an axial tensile load of 25 kN. The total elongation is 0.07 mm. Calculate the: a) axial stress ; b) axial strain.

**PROB-10**

The solid rod shown below is 30 mm in diameter and is acted upon by the forces as shown. Determine the stress state at point H and draw the stress element. Solve the problem by looking at point H from the top side.



**EQUATIONS:**

$$\begin{aligned} \epsilon &= \delta/L ; \sigma = P/A ; \sigma = E\epsilon ; \delta = \sum (P_i L_i) / (A_i E_i) ; \tau = (VQ) / (It) ; \\ q &= (VQ) / I ; \sigma = -(My) / I ; F_n = qs ; \tau = (Tr) / J ; A = bh ; A = \\ &= bh/2 ; A = \pi R^2 ; I = bh^3/12 ; J = \pi/2 (R_o^4 - R_i^4) ; I = \pi/4 (R_o^4 - R_i^4) \\ &; \epsilon = \alpha \Delta T ; Q = \sum A_i d_i ; d_i = |y_i - y_c| ; y_c = (\sum A_i y_i) / (\sum A_i) \\ &; \phi = \sum (T_i L_i) / (J_i G_i) ; I_c = \sum (I_{oi} + A_i d_i^2) ; dV/dx = -w(x) ; \\ dM/dx &= V ; d^2y/dx^2 = M/EI \end{aligned}$$